# MEAM 520 The Puma 260 and Project I

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Lecture 9: October 4, 2012



## A few good questions about DH parameters...



### FORWARD AND INVERSE KINEMATICS



Fig. 3.16 Elbow manipulator with shoulder offset

### The Denavit-Hartenberg Convention Page 78 in SHV (DHI) The axis x<sub>i</sub> is perpendicular to the axis z<sub>i-1</sub> (DH2) The axis x<sub>i</sub> intersects the axis z<sub>i-1</sub>



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+ New Post Q Search or add a post Question History:						
- PINNED	× 1	the instructors' answer, where instructors collectively	construct a single answer			
Form project teams & study groups! #pin • 1 Open Teammate Search	8/28/12	DH parameters work only when you follow the rules for placing the coordinate frames. It sounds like you have correctly identified the z-axes as the joint axes, but the origins you have chosen do not satisfy the DH conventions. I believe this is because the book contains an error on this point. The two DH rules laid out on page 78 of SHV are:				
- FAVORITES	*	(DUI) The suis will be norman disular to the suis =0.				
TODAY (DH1) The axis x1 is perpendicular to the axis zo (DH2) The axis x1 intersects the axis zo						
Confused about DH parameters I'm a little confused about how to do DH parameters for the following case: If I have revolute revolute arm, with dis #dh	1:25AM a	To follow the second rule, if two successive z-axes (e.g., z0 and z1) intersect, you must put the origin for frame 1 at the intersection of z0 and z1. In your example, this means you cannot move frame 1 up - its origin must be coincident with the origin of frame 0.				
YESTERDAY	• An instructor thinks this is a good question On page 82, the book describes what to do when "(iii) $z_{i-1}$ intersects $z_i$ : In this case $x_i$ is chosen normal to the plane formed by $z_i$ and $z_{i-1}$ . The positive direction of $x_i$ is arbitrary." This is all correct.					
What is 'zero configuration' mean? I am not sure about the definition. #homework3 #homework3	10:23PM	Then the book goes on to say, "The most natural choice for the origin $o_i$ in this case is at the point of intersection of $z_i$ and $z_{i-1}$ . However, any convenient point along the axis $z_i$ suffices." I think the book is wrong here. You may not pick any arbitrary location along $z_i$ because you must satisfy (DH2) from above ( $x_i$ must intersect $z_{i-1}$ ). Thus, the intersection between the two z-axes is the only allowable choice for the origin of frame i.				
OH parameters for elbow manipulato I was reading inverse kinematics in SHV and came across this robot on page 101 which has an offset on the shoulder. It s #dh	9:45PM	Please look this over and let me know if you think I am explaining things correctly. There is a chance I am just misinterpreting the book's guidance, but it seems pretty clear given the basic DH rules and the fact that one can't come up with a set of DH parameters for the situation you outlined in your question. Please write back with any clarifications or updates.				
HW3 PUMA260 Animation       3:03PM         In the code, it says plot the origin of the six       I						
we plot the origin #homework3		edit good answer 0 more -	34 minutes ago by Katherine J. Ku 2 edits 👻			
THIS WEEK followup discussions, for lingering questions and comments						
Matrix indexing and multiplication in the Hi, I'm wondering if there is a way to index matrix that you have multiplied without creating an intermediate variabl #matlab	. Mon a Si	Click to start a new followup discussion				
Private HW Drops	Mon	33 min Thomas Koletschka answered	What is 'zero configuration' in 4 min. 10 ho       4       84			
Views: Vi						

 $z_{i-1}$ ,  $z_i$  are parallel. Note that in both cases (ii) and (iii) the axes  $z_{i-1}$  and  $z_i$  are coplanar. This situation is in fact quite common, as we will see in Section 3.2.3. We now consider each of these three cases.

(i)  $z_{i-1}$  and  $z_i$  are not coplanar: If  $z_{i-l}$  and  $z_i$  are not coplanar, then there exists a unique shortest line segment from  $z_{i-1}$  to  $z_i$ , perpendicular to both  $z_{i-1}$  to  $z_i$ . This line segment defines  $x_i$ , and the point where it intersects  $z_i$  is the origin  $o_i$ . By construction, both conditions (DH1) and (DH2) are satisfied and the vector from  $o_{i-1}$  to  $o_i$  is a linear combination of  $z_{i-1}$  and  $x_i$ . The specification of frame *i* is completed by choosing the axis  $y_i$  to form a right-handed frame. Since assumptions (DH1) and (DH2) are satisfied, the homogeneous transformation matrix  $A_i$  is of the form given in Equation (3.10).

(ii)  $z_{i-1}$  is parallel to  $z_i$ : If the axes  $z_{i-1}$  and  $z_i$  are parallel, then there are infinitely many common normals between them and condition (DH1) does not specify  $x_i$  completely. In this case we are free to choose the origin  $o_i$ anywhere along  $z_i$ . One often chooses  $o_i$  to simplify the resulting equations. The axis  $x_i$  is then chosen either to be directed from  $o_i$  toward  $z_{i-1}$ , along the common normal, or as the opposite of this vector. A common method for choosing  $o_i$  is to choose the normal that passes through  $o_{i-1}$  as the  $x_i$ axis;  $o_i$  is then the point at which this normal intersects  $z_i$ . In this case,  $d_i$ would be equal to zero. Once  $x_i$  is fixed,  $y_i$  is determined, as usual by the right hand rule. Since the axes  $z_{i-1}$  and  $z_i$  are parallel,  $\alpha_i$  will be zero in this case.

(iii)  $z_{i-1}$  intersects  $z_i$ : In this case  $x_i$  is chosen normal to the plane formed by  $z_i$  and  $z_{i-1}$ . The positive direction of  $x_i$  is arbitrary. The most only natural choice for the origin  $o_i$  in this case is at the point of intersection of  $z_i$  and  $z_{i-1}$ . However, any convenient point along the axis  $z_i$  suffices. Note that in this case the parameter  $a_i$  will be zero.

This constructive procedure works for frames  $0, \ldots, n-1$  in an *n*-link robot. To complete the construction it is necessary to specify frame *n*. The final coordinate system  $o_n x_n y_n z_n$  is commonly referred to as the **end effector** or **tool frame** (see Figure 3.5). The origin  $o_n$  is most often placed symmetrically between the fingers of the gripper. The unit vectors along the  $x_n, y_n$ , and  $z_n$  axes are labeled as n, s, and a, respectively. The terminology arises from the fact that the direction a is the **approach** direction, in the sense that the gripper typically approaches an object along the a direction. Similarly the s direction is the **sliding** direction, the direction along which

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## Questions ?

## **Inverse Orientation Kinematics**







Given rotation matrix **R**, find the joint angles that put the end-effector in the desired orientation.



$T_{6}^{3}$	= .	$A_4 A_5 A_6$			
	q	$\left[\begin{array}{cc} R_6^3 & o_6^3 \\ 0 & 1 \end{array}\right]$			
		$c_4 c_5 c_6 - s_4 s_6$	$-c_4c_5s_6 - s_4c_6$	$c_{4}s_{5}$	$c_4s_5d_6$
		$s_4c_5c_6 + c_4s_6$	$-s_4c_5s_6 + c_4c_6$	$s_{4}s_{5}$	$s_4s_5d_6$
	_	$-s_5c_6$	$s_{5}s_{6}$	$c_5$	$c_5 d_6$
		0	0	0	1

Define a set of three <code>intermediate</code> angles,  $\phi, heta, \psi$  , to go from 0 
ightarrow 3



step I:rotate by  $\phi$  about  $z_0$ 



step 2: rotate by  $\theta$  about  $y_1$ 



step 3: rotate by  $\psi$  about  $z_2$ 



(**post**-multiply using the **basic rotation matrices**)

$$\mathbf{R} = \mathbf{R}_{z,\phi} \; \mathbf{R}_{y, heta} \; \mathbf{R}_{z,\psi}$$

$$= \begin{bmatrix} c_{\phi} & -s_{\phi} & 0 \\ s_{\phi} & c_{\phi} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} c_{\theta} & 0 & s_{\theta} \\ 0 & 1 & 0 \\ -s_{\theta} & 0 & c_{\theta} \end{bmatrix} \begin{bmatrix} c_{\psi} & -s_{\psi} & 0 \\ s_{\psi} & c_{\psi} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{array}{cccc} c_{\phi}c_{\theta}c_{\psi} - s_{\phi}s_{\psi} & -c_{\phi}c_{\theta}s_{\psi} - s_{\phi}c_{\psi} & c_{\phi}s_{\theta} \\ s_{\phi}c_{\theta}c_{\psi} + c_{\phi}s_{\psi} & -s_{\phi}c_{\theta}s_{\psi} + c_{\phi}c_{\psi} & s_{\phi}s_{\theta} \\ & -s_{\theta}c_{\psi} & s_{\theta}s_{\psi} & c_{\theta} \end{array}$$

$$T_{6}^{3} = A_{4}A_{5}A_{6}$$

$$= \begin{bmatrix} R_{6}^{3} & o_{6}^{3} \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} c_{4}c_{5}c_{6} - s_{4}s_{6} & -c_{4}c_{5}s_{6} - s_{4}c_{6} & c_{4}s_{5} & c_{4}s_{5}d_{6} \\ s_{4}c_{5}c_{6} + c_{4}s_{6} & -s_{4}c_{5}s_{6} + c_{4}c_{6} & s_{4}s_{5} & s_{4}s_{5}d_{6} \\ -s_{5}c_{6} & s_{5}s_{6} & c_{5} & c_{5}d_{6} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\theta_4 = \phi \qquad \theta_5 = \theta \qquad \theta_6 = \psi$$

$$= \begin{bmatrix} c_{\phi}c_{\theta}c_{\psi} - s_{\phi}s_{\psi} & -c_{\phi}c_{\theta}s_{\psi} - s_{\phi}c_{\psi} & c_{\phi}s_{\theta} \\ s_{\phi}c_{\theta}c_{\psi} + c_{\phi}s_{\psi} & -s_{\phi}c_{\theta}s_{\psi} + c_{\phi}c_{\psi} & s_{\phi}s_{\theta} \\ -s_{\theta}c_{\psi} & s_{\theta}s_{\psi} & c_{\theta} \end{bmatrix}$$

The book explains how to calculate the three angles given **R**: see SHV pages 55-56

#### 2.5. PARAMETERIZATIONS OF ROTATIONS

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To find a solution for this problem we break it down into two cases. First, suppose that not both of  $r_{13}$ ,  $r_{23}$  are zero. Then from Equation (2.26) we deduce that  $s_{\theta} \neq 0$ , and hence that not both of  $r_{31}$ ,  $r_{32}$  are zero. If not both  $r_{13}$  and  $r_{23}$  are zero, then  $r_{33} \neq \pm 1$ , and we have  $c_{\theta} = r_{33}$ ,  $s_{\theta} = \pm \sqrt{1 - r_{33}^2}$  so

$$\theta = \operatorname{Atan2}\left(r_{33}, \sqrt{1 - r_{33}^2}\right)$$
 (2.28)

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or

$$= \operatorname{Atan2}\left(r_{33}, -\sqrt{1 - r_{33}^2}\right) \tag{2.29}$$

where the function Atan2 is the **two-argument arctangent function** defined in Appendix A.

If we choose the value for  $\theta$  given by Equation (2.28), then  $s_{\theta} > 0$ , and

$$\phi = A \tan 2(r_{13}, r_{23})$$
(2.30)  

$$\psi = A \tan 2(-r_{31}, r_{32})$$
(2.31)

If we choose the value for  $\theta$  given by Equation (2.29), then  $s_{\theta} < 0$ , and

$$\phi = A \tan 2(-r_{13}, -r_{23})$$
(2.32)  

$$\psi = A \tan 2(r_{31}, -r_{32})$$
(2.33)

Thus, there are two solutions depending on the sign chosen for  $\theta$ .

If  $r_{13} = r_{23} = 0$ , then the fact that R is orthogonal implies that  $r_{33} = \pm 1$ , and that  $r_{31} = r_{32} = 0$ . Thus, R has the form

$$R = \begin{bmatrix} r_{11} & r_{12} & 0\\ r_{21} & r_{22} & 0\\ 0 & 0 & \pm 1 \end{bmatrix}$$
(2.34)

If  $r_{33} = 1$ , then  $c_{\theta} = 1$  and  $s_{\theta} = 0$ , so that  $\theta = 0$ . In this case, Equation (2.26) becomes

$$\begin{bmatrix} c_{\phi}c_{\psi} - s_{\phi}s_{\psi} & -c_{\phi}s_{\psi} - s_{\phi}c_{\psi} & 0\\ s_{\phi}c_{\psi} + c_{\phi}s_{\psi} & -s_{\phi}s_{\psi} + c_{\phi}c_{\psi} & 0\\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} c_{\phi+\psi} & -s_{\phi+\psi} & 0\\ s_{\phi+\psi} & c_{\phi+\psi} & 0\\ 0 & 0 & 1 \end{bmatrix}$$

Thus, the sum  $\phi + \psi$  can be determined as

$$\phi + \psi = \operatorname{Atan2}(r_{11}, r_{21}) = \operatorname{Atan2}(r_{11}, -r_{12})$$
(2.35)

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#### CHAPTER 2. RIGID MOTIONS

Since only the sum  $\phi + \psi$  can be determined in this case, there are infinitely many solutions. In this case, we may take  $\phi = 0$  by convention. If  $r_{33} = -1$ , then  $c_{\theta} = -1$  and  $s_{\theta} = 0$ , so that  $\theta = \pi$ . In this case Equation (2.26) becomes

$$\begin{bmatrix} -c_{\phi-\psi} & -s_{\phi-\psi} & 0\\ s_{\phi-\psi} & c_{\phi-\psi} & 0\\ 0 & 0 & -1 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & 0\\ r_{21} & r_{22} & 0\\ 0 & 0 & -1 \end{bmatrix}$$
(2.36)

The solution is thus

$$\phi - \psi = \operatorname{Atan2}(-r_{11}, -r_{12}) \tag{2.37}$$

As before there are infinitely many solutions.

#### 2.5.2 Roll, Pitch, Yaw Angles

A rotation matrix R can also be described as a product of successive rotations about the principal coordinate axes  $x_0, y_0$ , and  $z_0$  taken in a specific order. These rotations define the **roll**, **pitch**, and **yaw** angles, which we shall also denote  $\phi, \theta, \psi$ , and which are shown in Figure 2.11.



Figure 2.11: Roll, pitch, and yaw angles.

We specify the order of rotation as x - y - z, in other words, first a yaw about  $x_0$  through an angle  $\psi$ , then pitch about the  $y_0$  by an angle  $\theta$ , and finally roll about the  $z_0$  by an angle  $\phi$ .<sup>4</sup> Since the successive rotations are

<sup>4</sup>It should be noted that other conventions exist for naming the roll, pitch, and yaw angles.

## Questions ?

# Project I Light Painting with the Puma 260

- The Puma 260 has been equipped with a tri-color LED end-effector.
- Taking long-exposure photos of the Puma moving in a darkened room produces works of art known as "light paintings."
- Your job is to work in a team of three to create a beautiful Puma light painting.





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http://youtube.googleapis.com/v/eJLGjaXbzgk

+ http://youtube.googleapis.com/v/eJLGjaXbzgk

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### PUMA Light Painting - Team 8



## What knowledge do you need to do this project?



Jonathan Fiene



#### FEATURES

The Series 200 is the most compact model in the UNIMATE PUMA line of electrically driven industrial robots. With an 18-inch reach and 2.2-pound payload capacity, the PUMA Series 200 robot is designed for medium to high-speed assembly and materials handling applications. Its capabilities are particularly suited to the requirements of electronics and other industries where lightweight parts handling is highly repetitive, fast and precise.

#### EASE OF USE

VAL<sup>™</sup>a revolutionary advance in robot control systems, is used to control and program PUMA robots. The system uses an LSI-11 as a central processing unit and communicates with individual joint processors for servo control of robot arm motions. The results are ease in set up, high-tolerance repeatability, and greater application versatility.



VAL combines a sophisticated, easy to use robot programming capability with advanced serve control methods. Intuitive English language instruction provides fast, efficient program generation and editing capabilities. All serve- path computations are performed in real time, which makes it possible to interface with sensory-based systems.

#### EASE OF INSTALLATION

PUMA 200 robots are easily integrated into existing production lines because of the ease with which they are programmed. In addition, the robot can be easily and quickly reprogrammed for changes in the product or production process.

Programs can be written either on- or off-line using a CRT or teletype terminal, or they can be generated manually by guiding the robot arm through program paths using a microprocessor-based teach pendant With either method, position data can be added or changed by key input, manual control or floppy disk input without affecting the overall task program.

VAL reduces memory requirements and permits complex programs, such as palletizing routines, to be easily written with a minimum number of taught positions.

Significant time savings can also be realized by integrating predefined subroutines and tasks into complex operations. These tasks can also be stored on floppy disks to build a library of routines, and even whole programs, that can be loaded into the memory of any PUMA controller so that specific tasks and repetitive routines need to be written only once.

With VAL, the Series 200 can also respond to fluctuations in the rate or other parameters of on going production processes. Since all servo-path computations are performed in real time, changes in the arm path, or even task sequencing, can be initiated by feedback from various sensors and vision systems. As a result, the 200 can interact flexibly and efficiently as part of a large and complex manufacturing system.

#### APPLICATIONS

With its high speed, repeatability, and flexibility the PUMA 200 robot is suited to a wide range of small parts-handling applications, and VAL control makes it easy to design application programs to carry out the most difficult robotic tasks.

Current assembly applications include automotive instrument panels, small electric motors, printed circuit boards, subassemblies for radios, television sets, appliances and more. Other applications include packaging functions in the pharmaceutical, personal care, and food industries. Palletizing of small parts, inspection, and electronic parts handling in the computer, aero space and defense industries round out the present installed base.



## **Unimate**<sup>®</sup>

PUMA<sup>®</sup> Mark II Robot

200 Series Equipment Manual for VAL<sup>™</sup> II and VAL<sup>™</sup> PLUS Operating Systems 398V1

Unimation

A Westinghouse Company

Unimation Incorporated Shelter Rock Lane Danbury, Connecticut 06810

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Figure 2-1. PUMA Dimensions - Installation





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## What does the Puma's workspace look like?



## How does the Puma work?









# First Step in Project I

Derive full inverse kinematics for the Puma 260

Given desired x, y, z position of LED and Euler angles for the end-effector, plus the current joint angles of the robot, calculate all the joint angles needed to reach the new desired configuration

Full assignment and MATLAB starter code will be distributed around Tuesday of next week

You will do this in teams of three

## **Team Formation**

You will work in a team of 3 (33 teams of 3, only one team of 4)

Each team must have at least one undergraduate and at least one graduate student. Submatriculants count as undergraduates. (52 undergrads, 51 grads)

Try to have two MEAM students and one non-MEAM student on each team (71 MEAM, 33 non-MEAM)

Pick your team by 5pm on Thursday, October 11 (one week from today)

## Speed Meeting Activity

Stand up, and leave your stuff where it is.

All undergraduates stand around the edges of the room.

Grad students - go stand in front of an undergraduate.

Introduce yourselves: name, major, favorite robot.

Rotate! Rotate! Rotate! Rotate!