



Gradient Blending



How to blend two images?

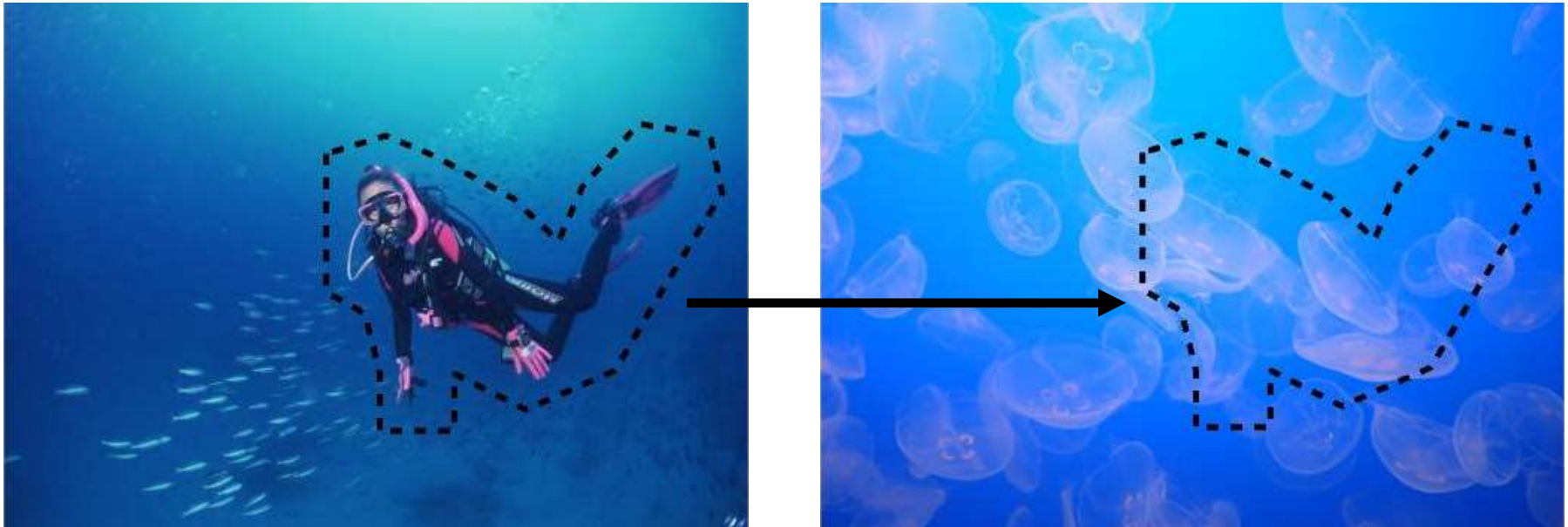


image blending: image surgery...

- cutting from one image (which we will cover in details on segmentation)
- reconstructing onto the new image

Blend = Cut and Paste images

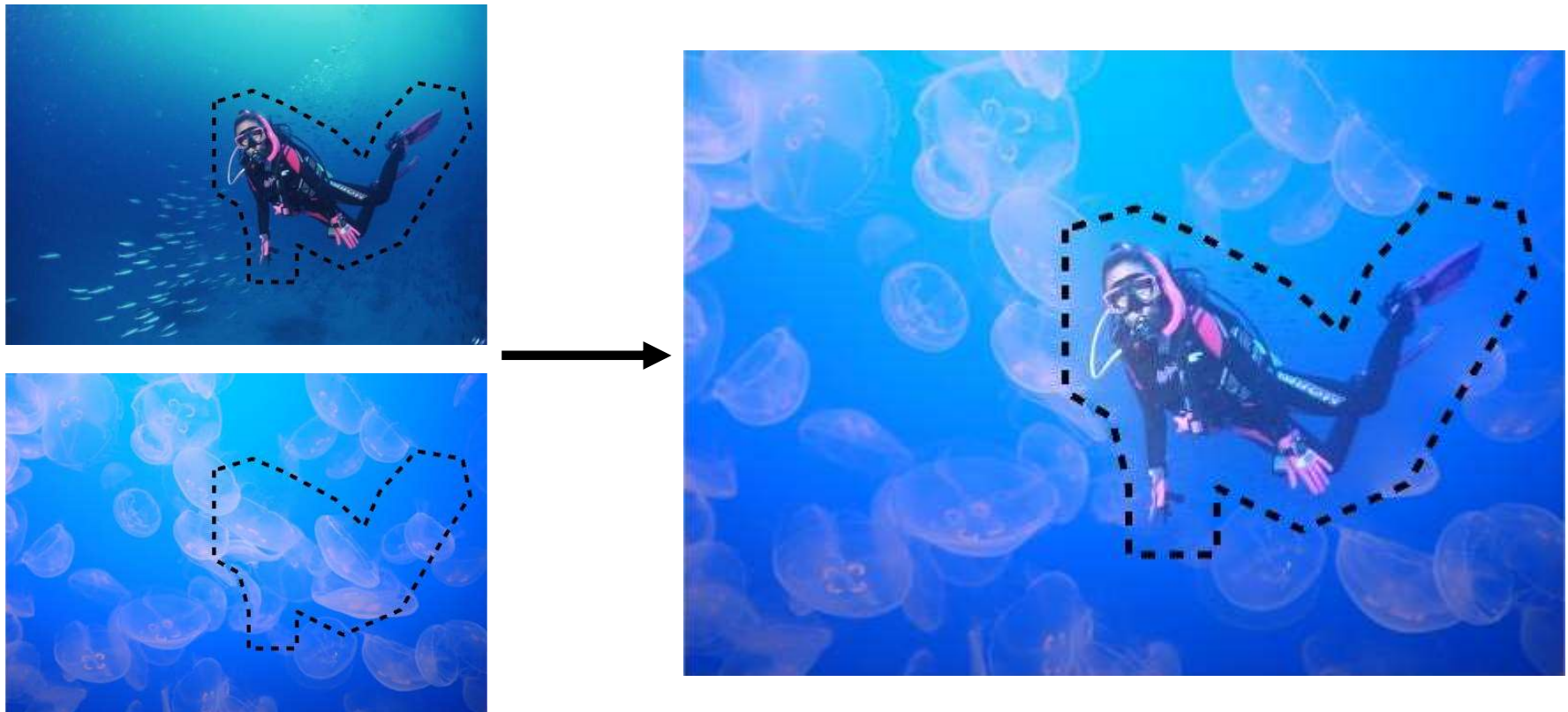
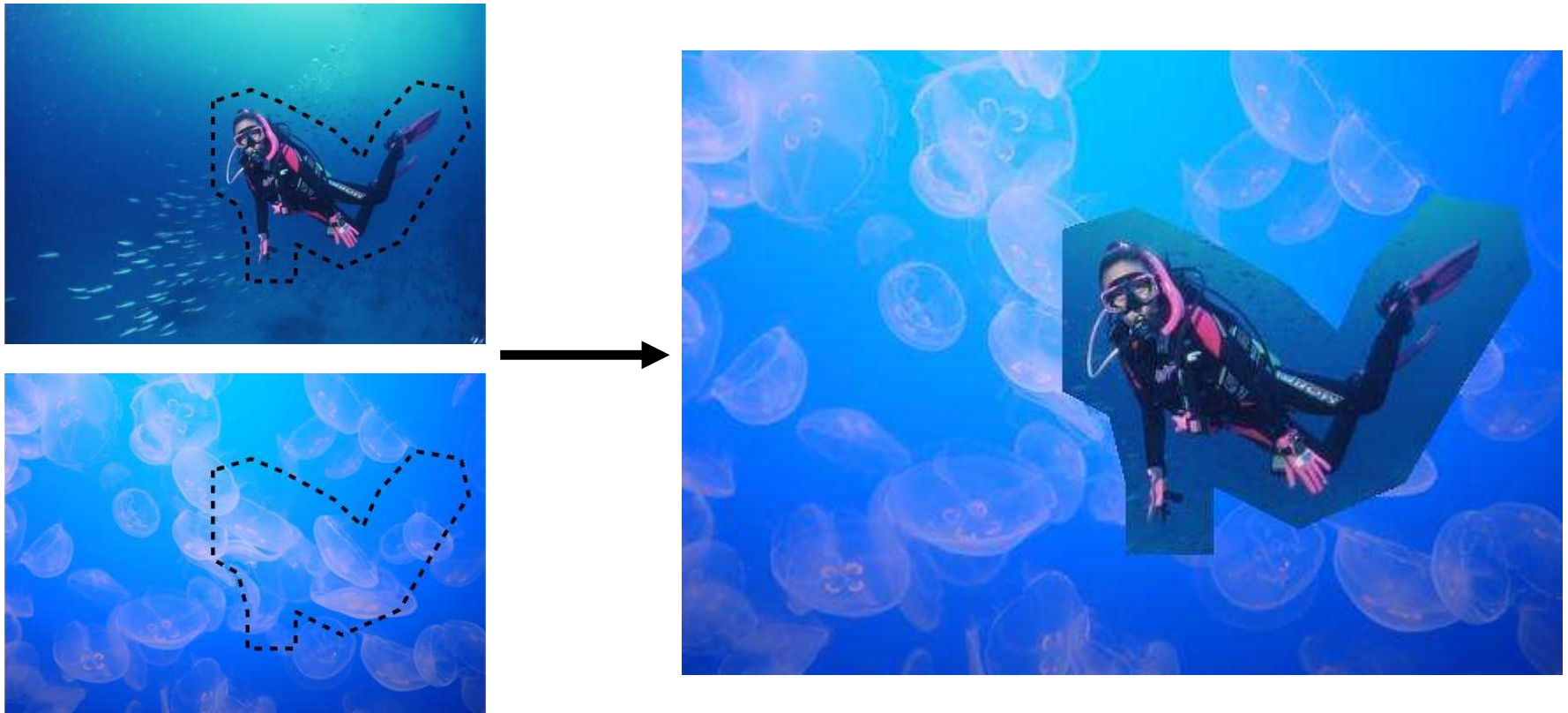


Image blending is an art of ...

faking images, hiding evidence of image surgery, making it look natural

Direct Copy and Paste

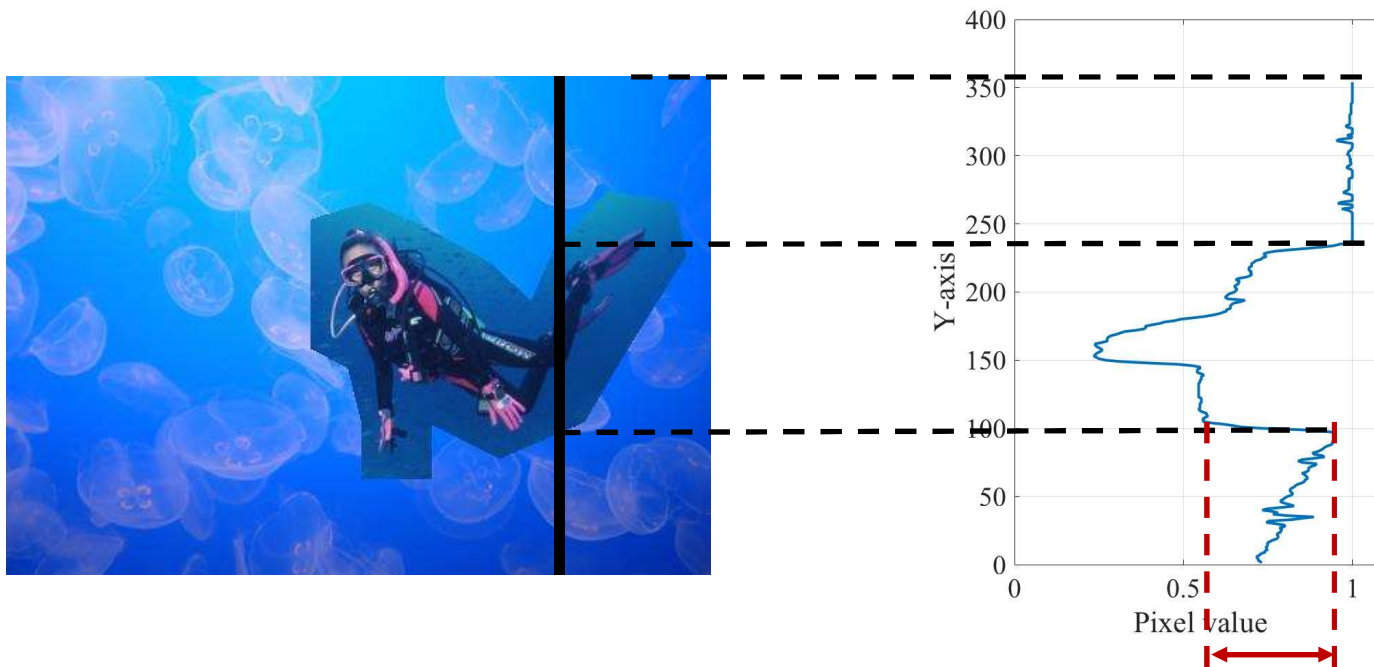


Direct attempt: not so good!

-- we created an artificial boundary between the pasted region

Challenge: color and brightness mismatch

Blue channel value of the vertical line



Big change in intensity

- Big change in intensity creates new image boundary...
- any ideas on how to remove that boundary?

Alpha blending

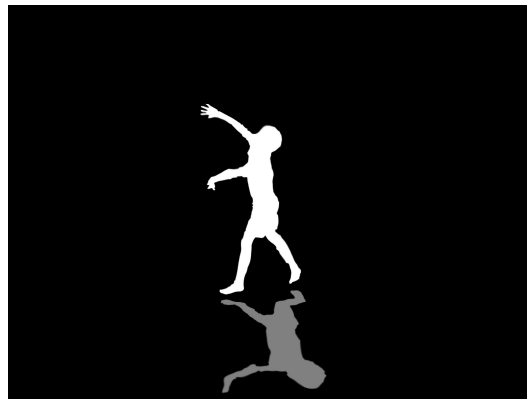
Alpha channel encodes the transparency of the object



Alpha blending



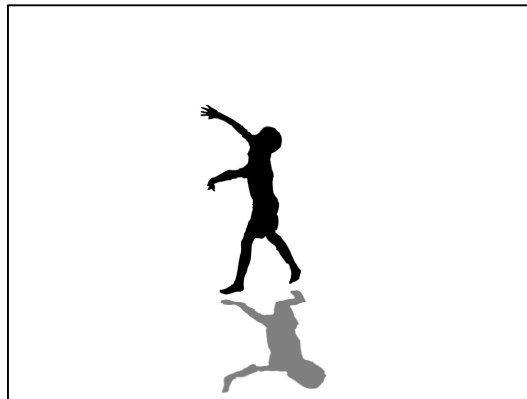
×



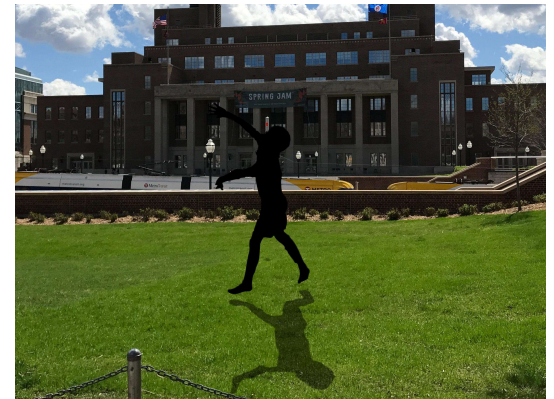
=



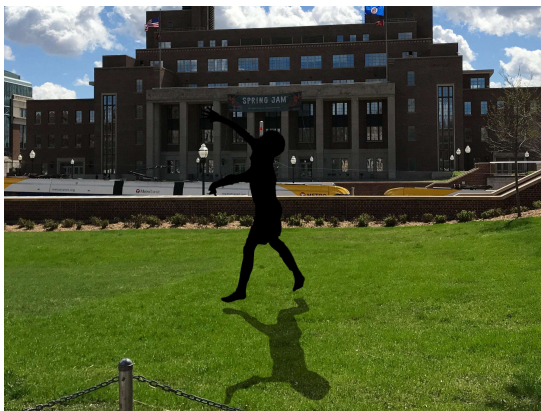
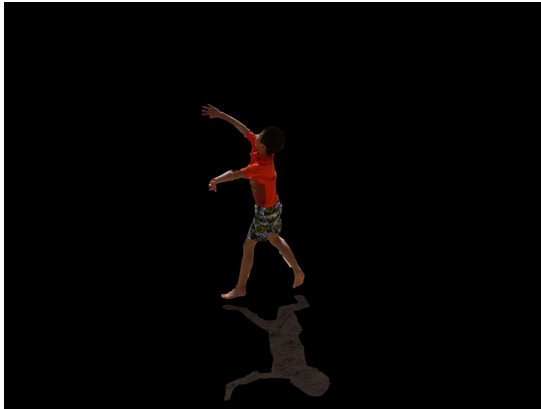
×



=

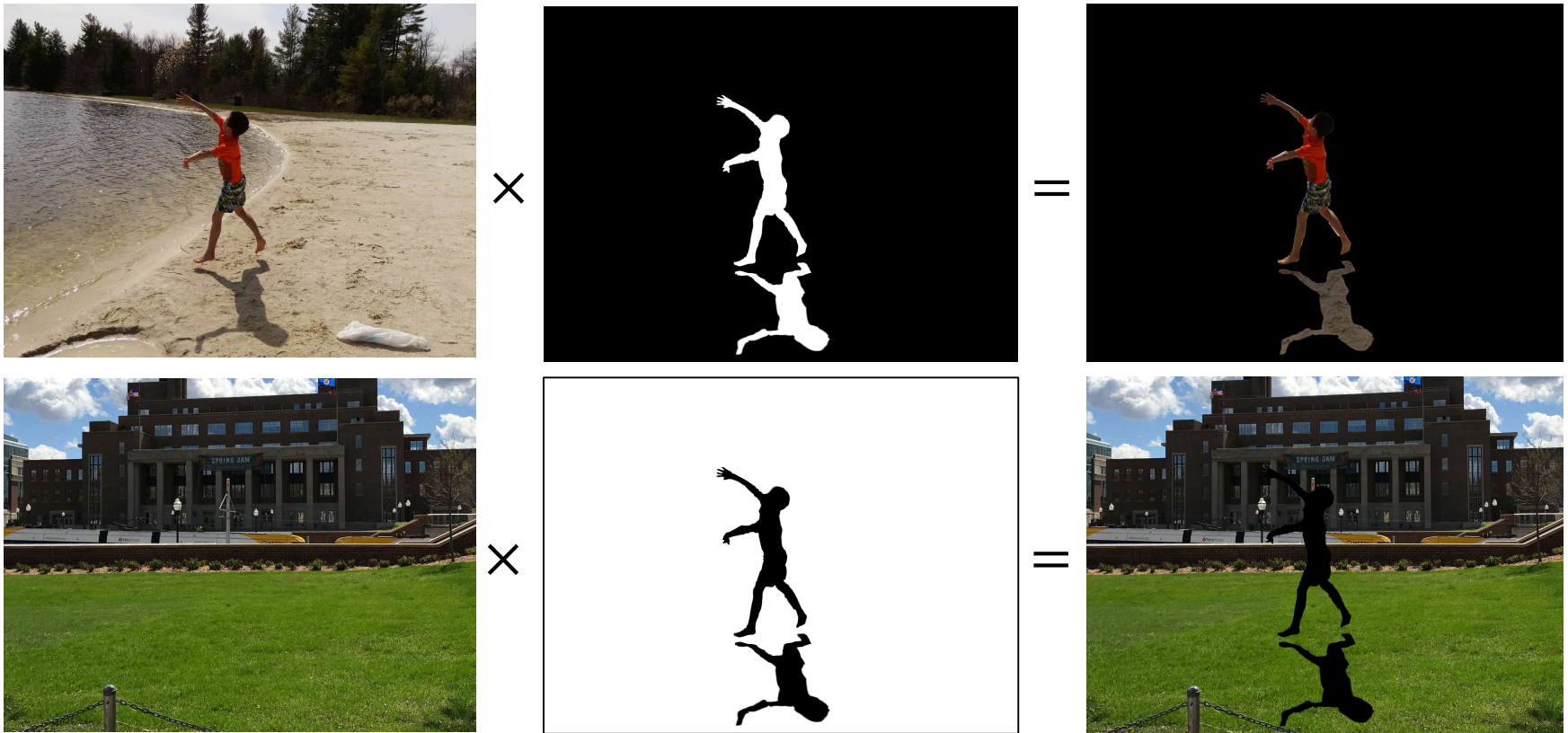


Alpha blending

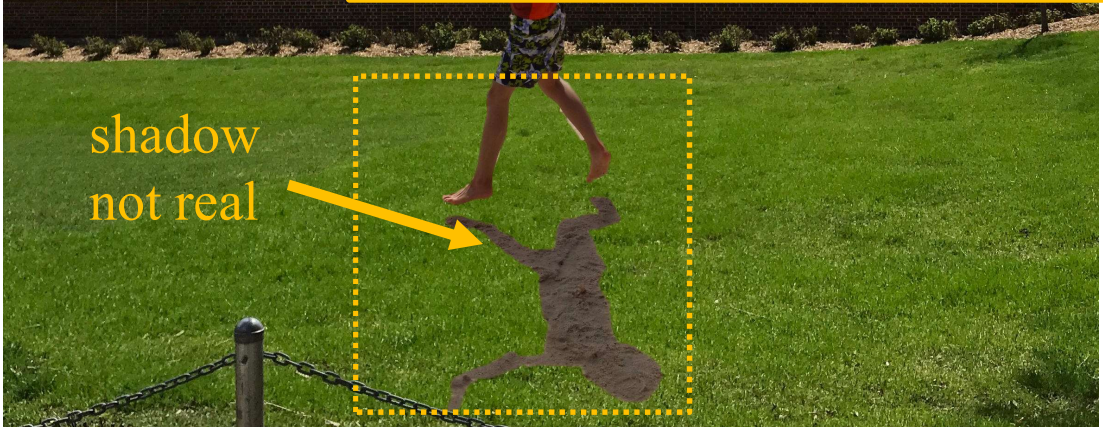
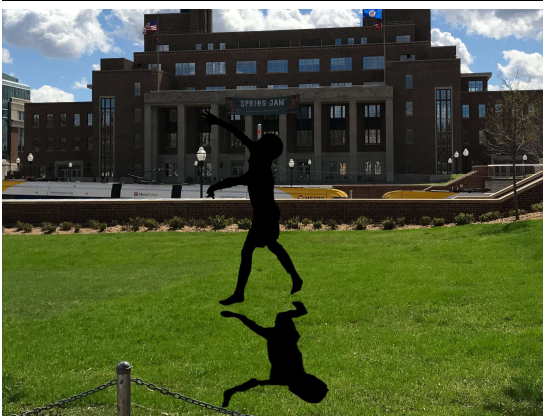
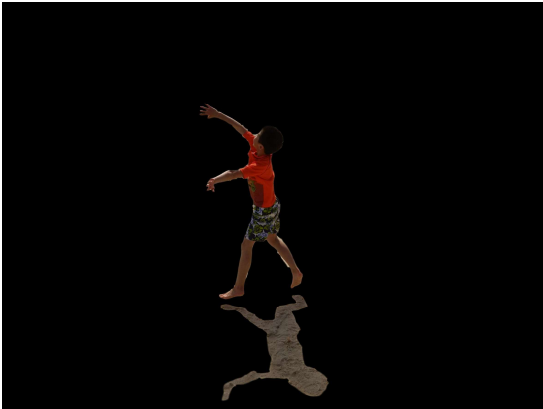


Alpha blending

Copy - paste is a special kind of alpha blending – binary mask

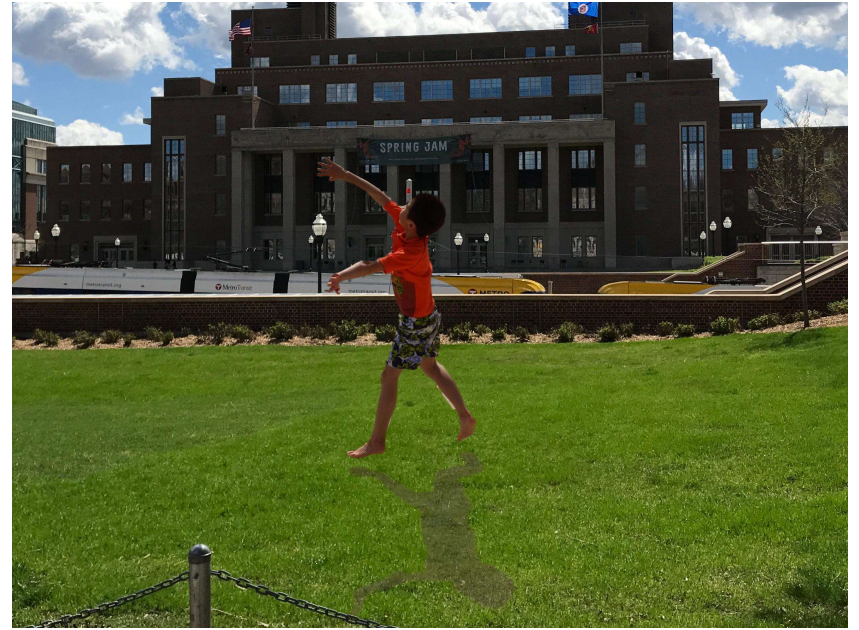








copy - paste



alpha blending

Alpha blending can deal with transparent objects

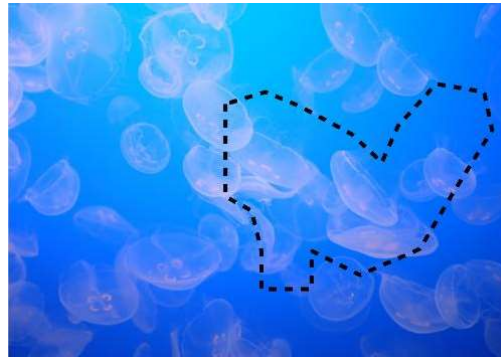
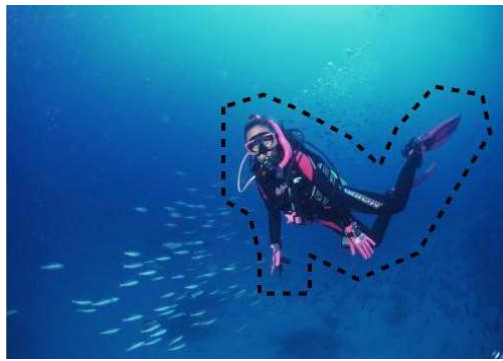


copy - paste



alpha blending

Alpha blending hacking



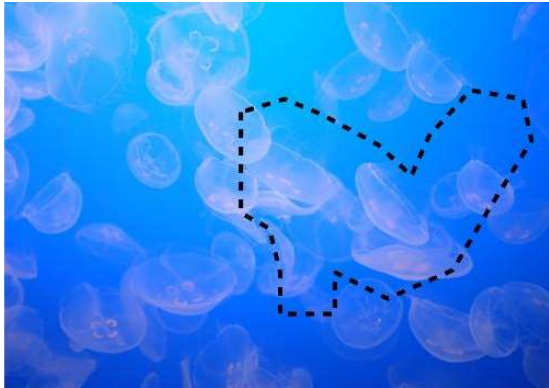
×

+

×

=





copy - paste

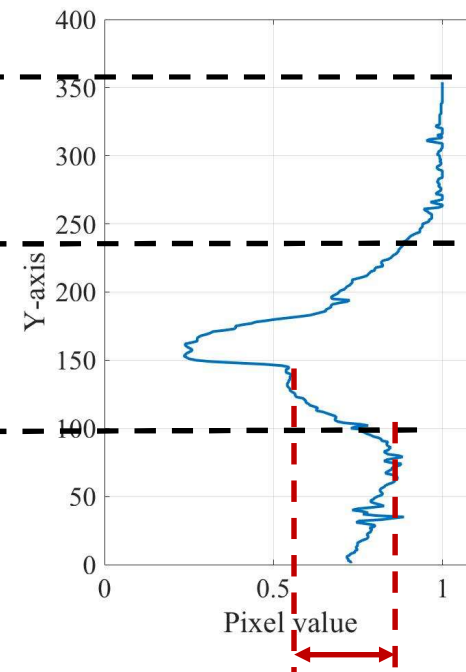


Alpha blending



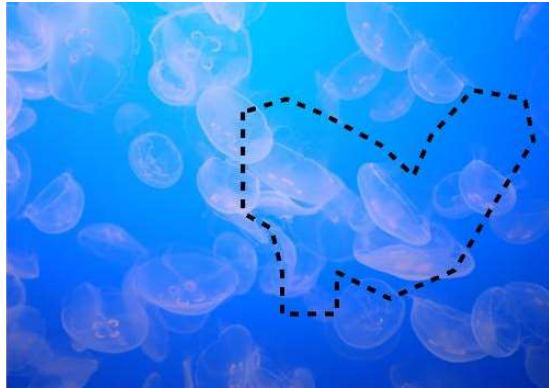
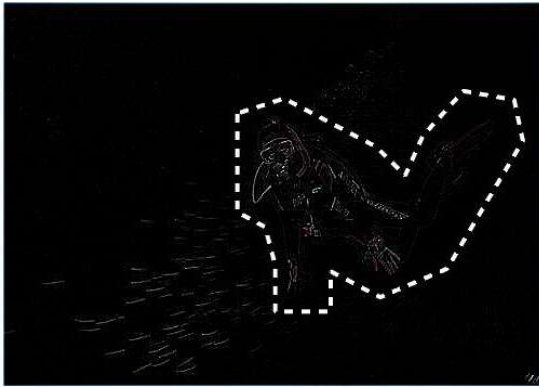
Alpha Blending

Blue channel value of the vertical line



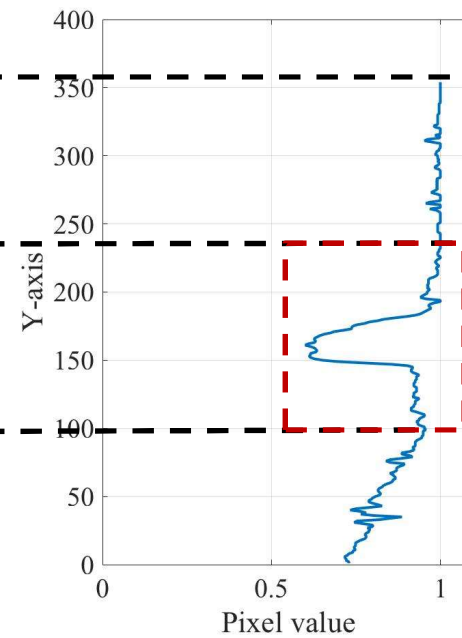
Continuous change,
but still a visually un-natural pattern in intensity

Solution: Copy only gradient + Recreate



Gradient Blending: No more intensity change!

Blue channel value of the vertical line



Smooth transition

Image Blending



copy - paste



alpha blending



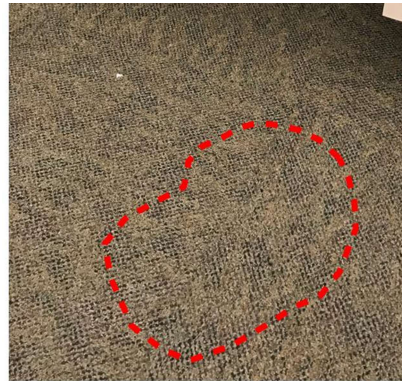
Gradient blending

Results of gradient blending

Source (figure)



Target (background)



Result



Color of the hat blends into the background

-- successful image surgery... with interesting side-affect

Gradient Blending



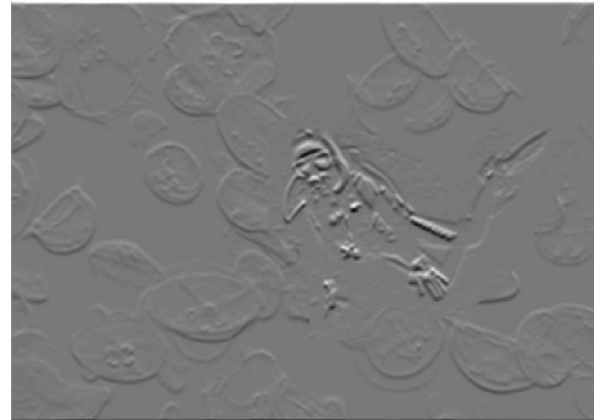
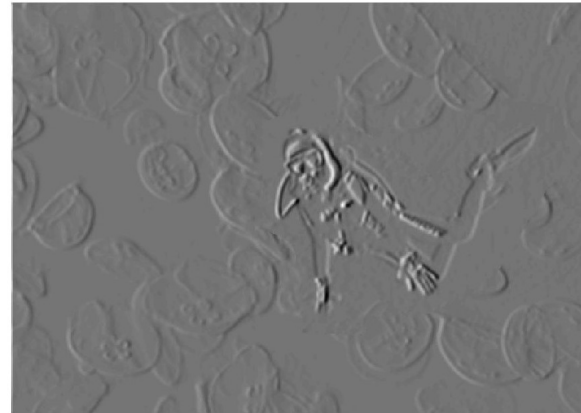
Gradient Blending



Gradient Blending



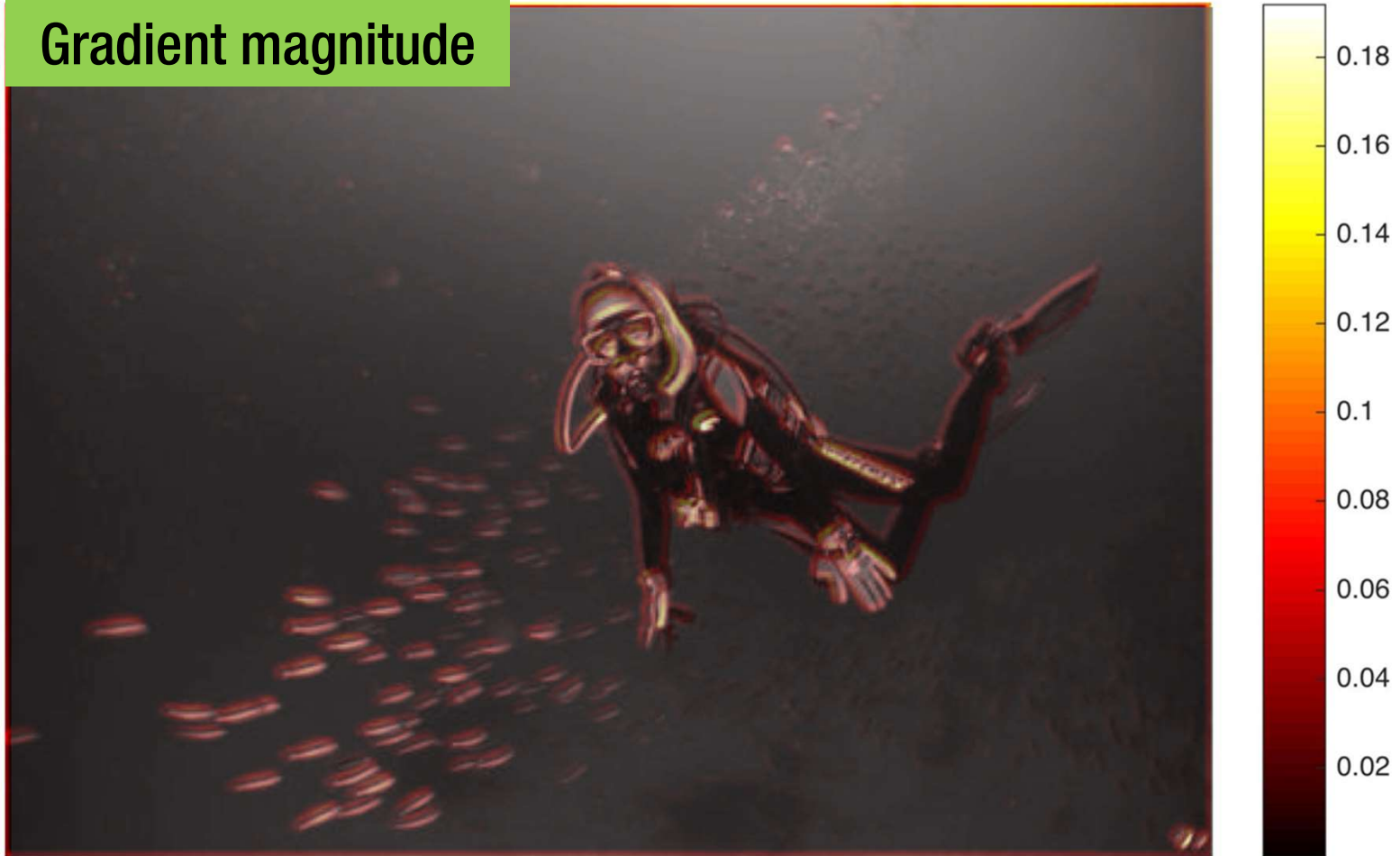
Why use the
gradients to
recreate images



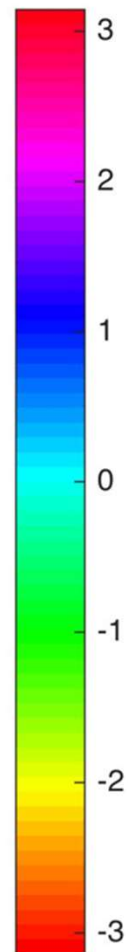
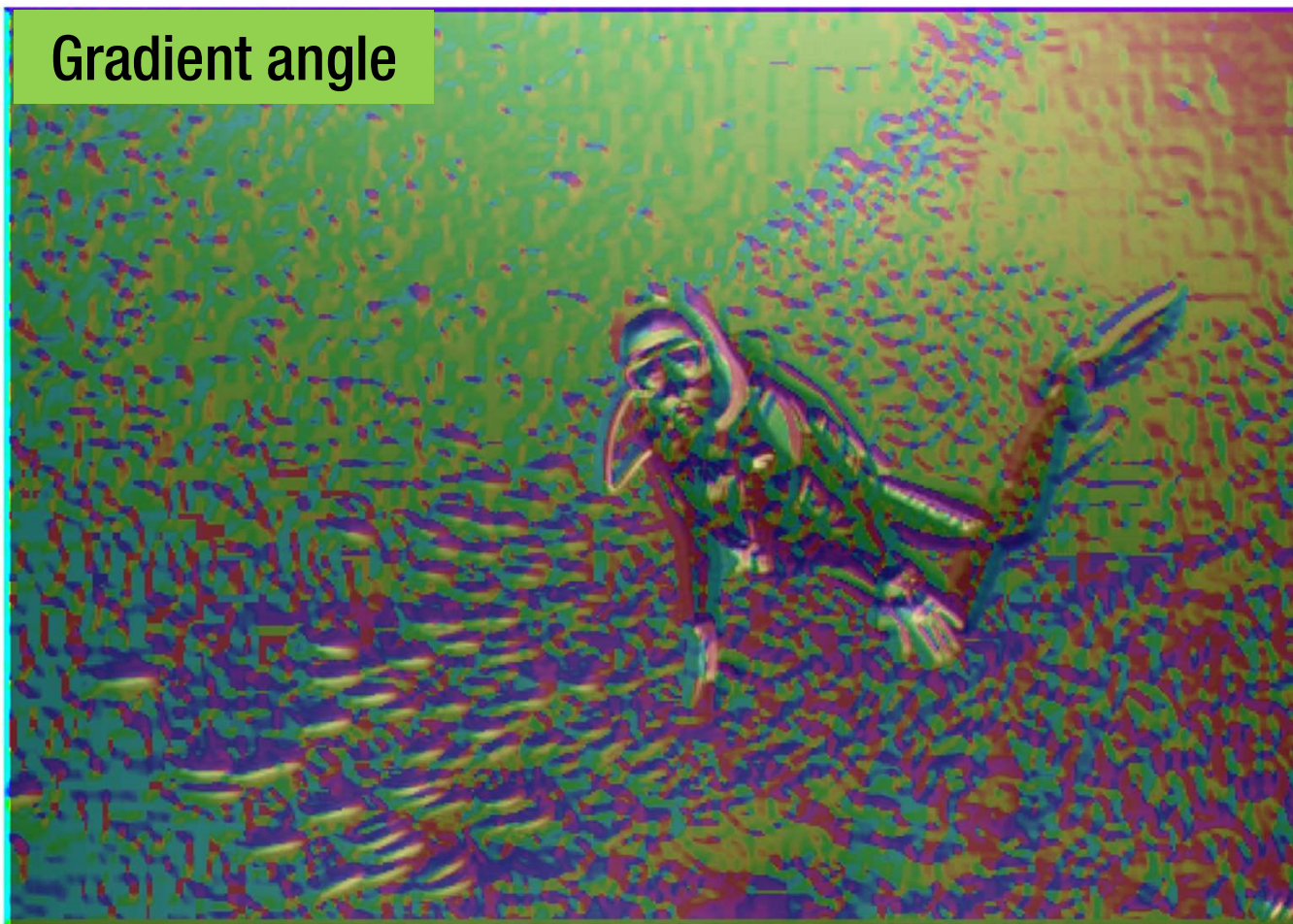
Source Image



Gradient magnitude

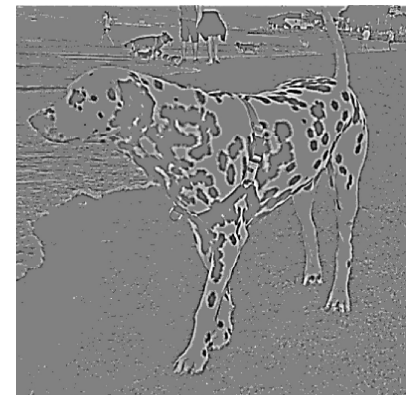
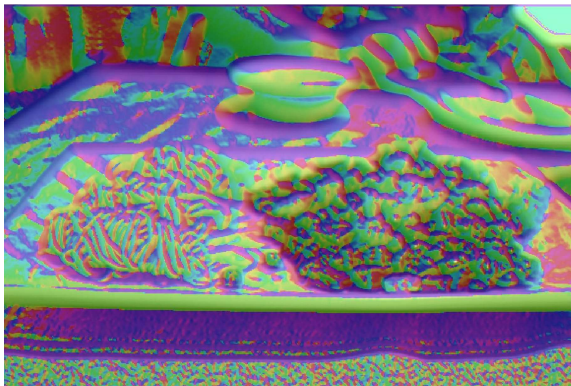


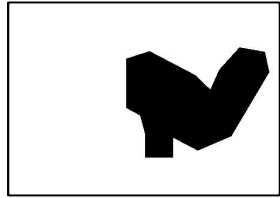
Gradient angle



Gradients domain

- Gradient captures everything important about shape and shading
- It contains the microscope texture of the object.
- It encodes subtle changes of illumination.
- In Pyramid Blending, we decomposed our image into 2nd derivatives (Laplacian) which encodes the shape perception.





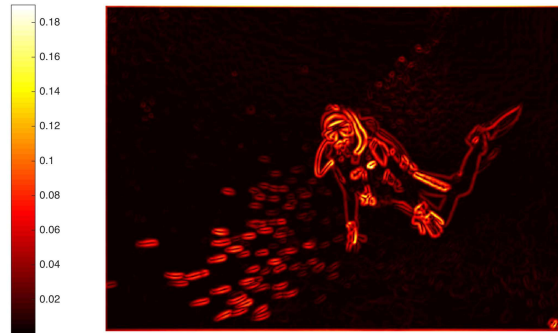
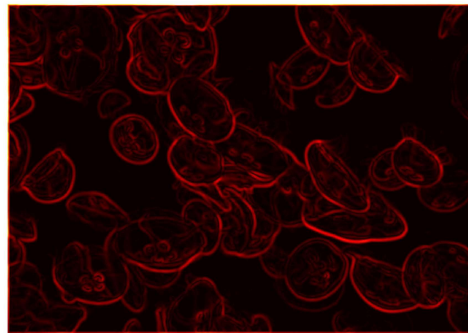
×



+

×

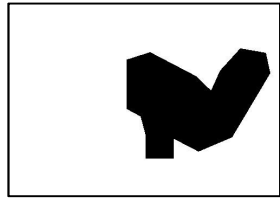
Blending Magnitude



=



- We blend the gradient magnitude, to create a seamless ‘edge’ image



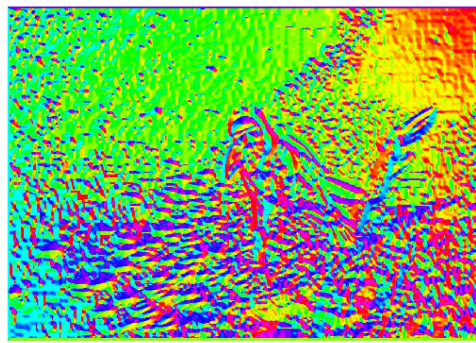
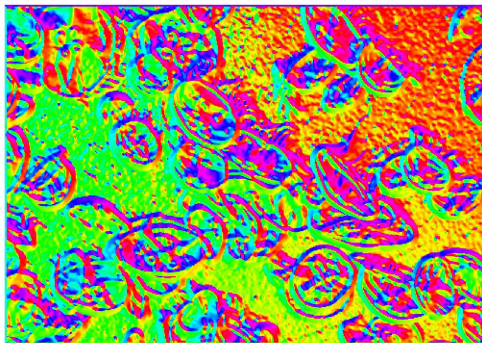
×



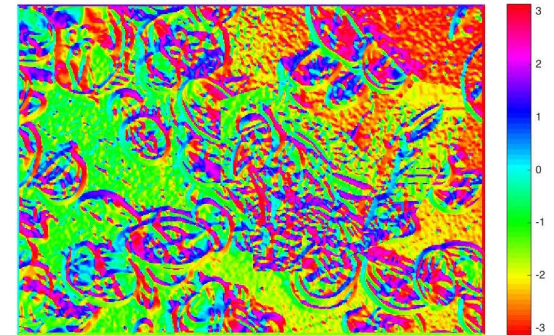
+

×

Blending the
Gradient angle



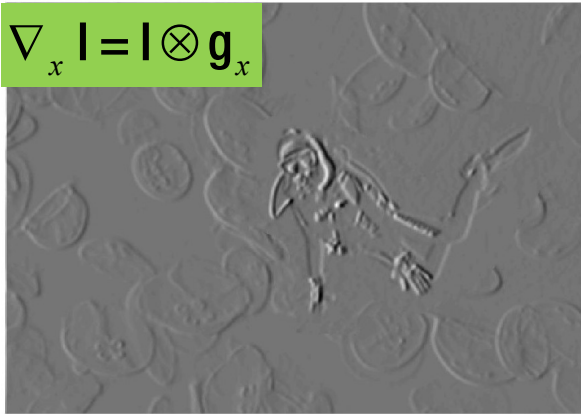
=



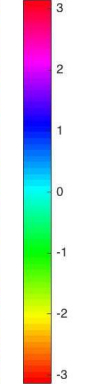
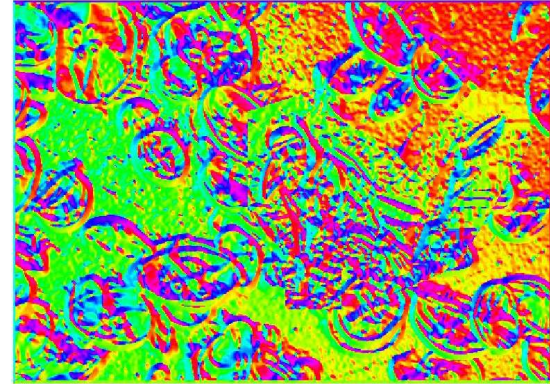
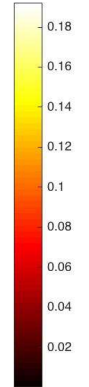
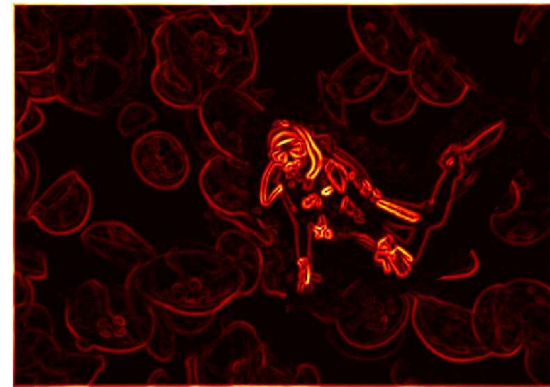
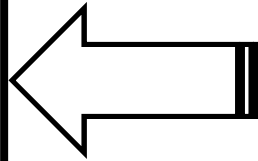
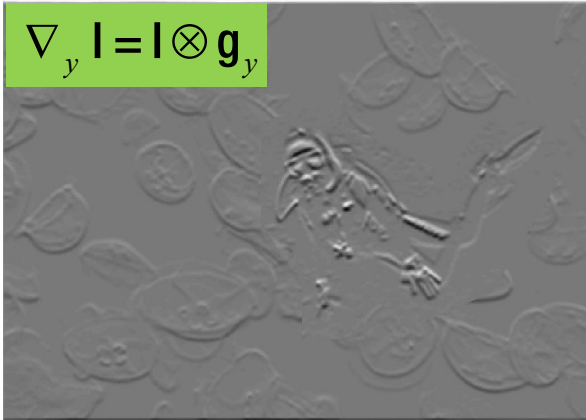
- We blend the gradient angle images, to make sure both the microscopic texture, shape of object boundary, and the illumination changes are smoothly integrated.

Image gradients blending

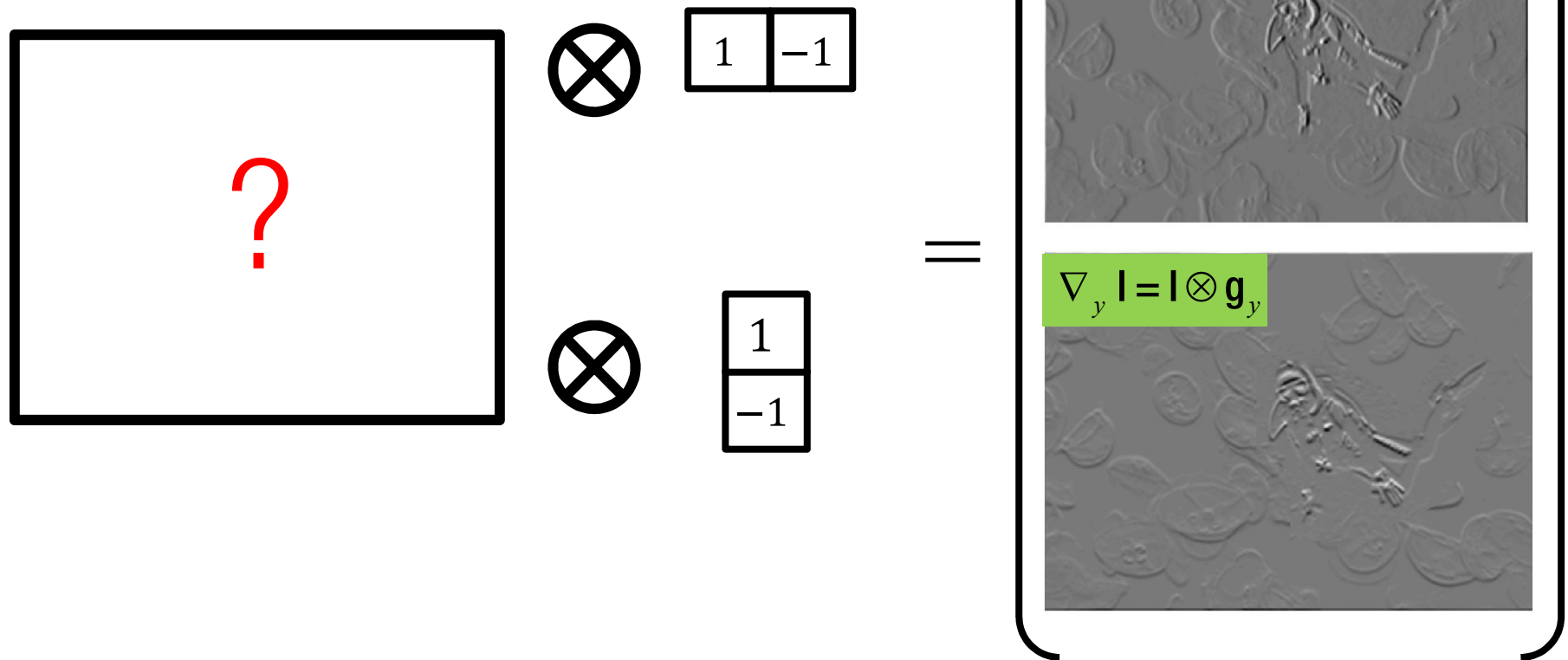
$$\nabla_x I = I \otimes g_x$$



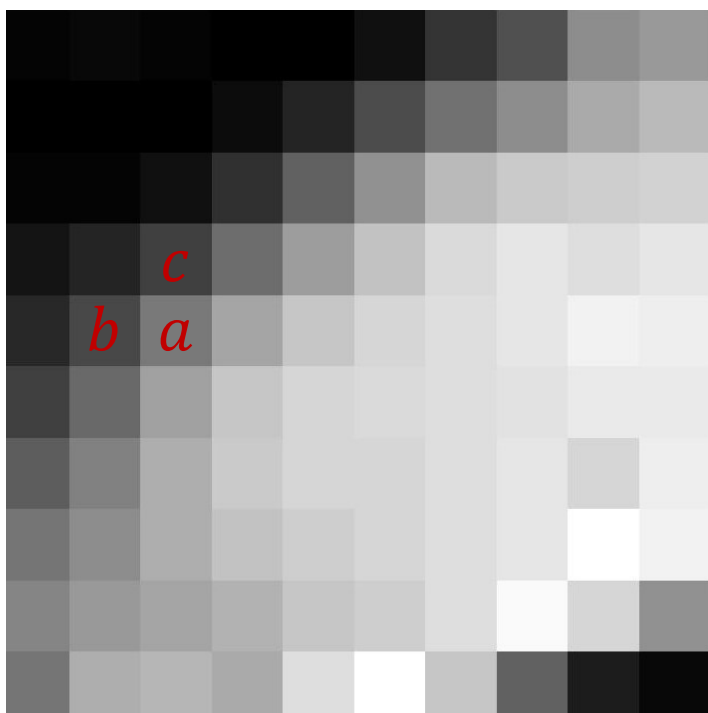
$$\nabla_y I = I \otimes g_y$$



How to recreate the original image from gradient?

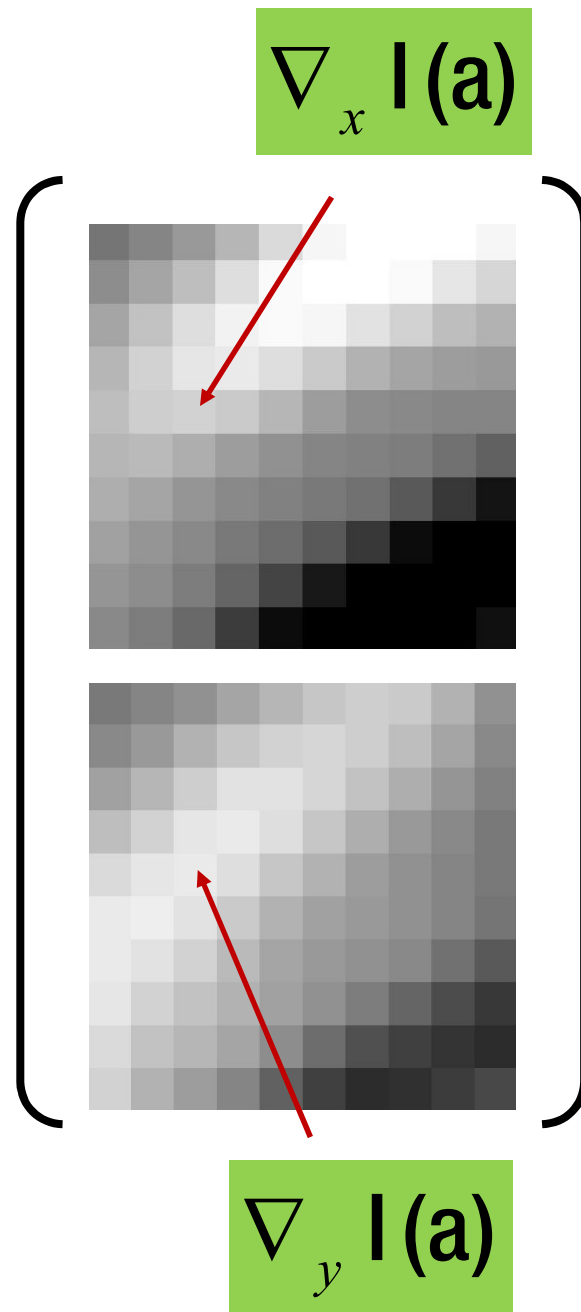


zoom in a small patch



$$\otimes \begin{bmatrix} 1 & -1 \end{bmatrix}$$

$$\otimes \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

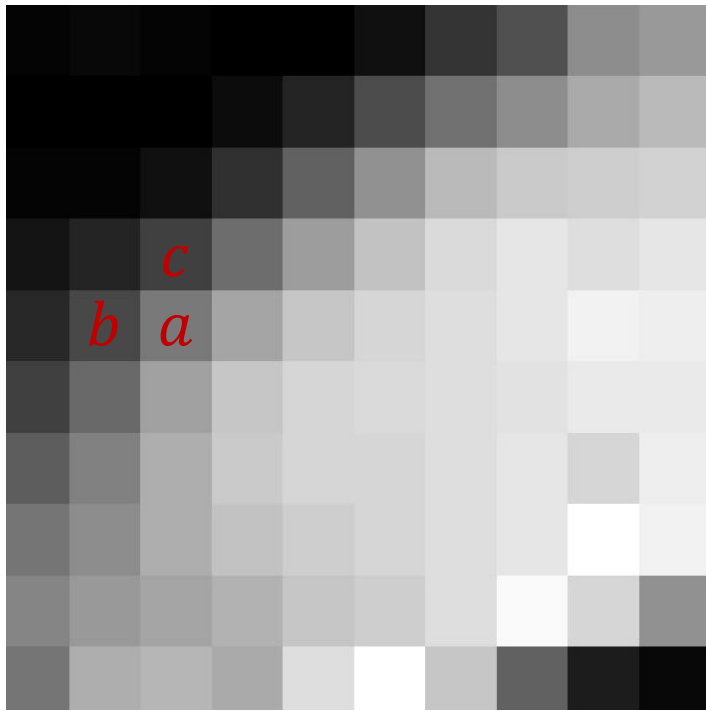


or

$$\begin{bmatrix} a \\ b \end{bmatrix} - \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} a-b \\ b-a \end{bmatrix} \quad \nabla_x I(a)$$

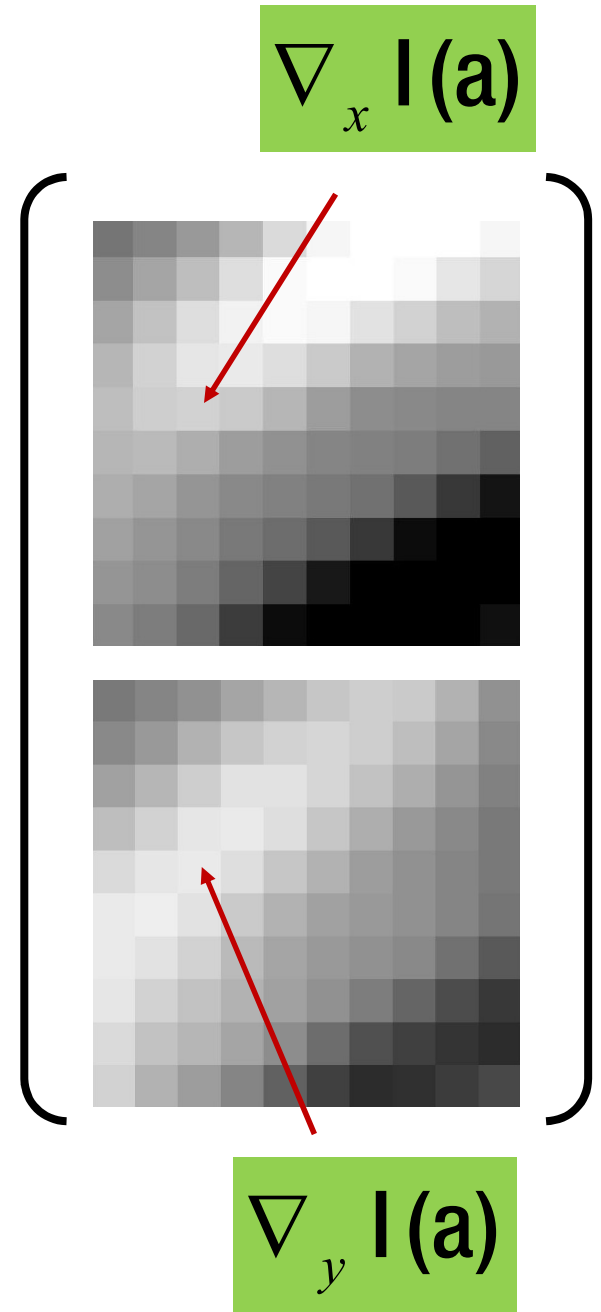
$$\begin{bmatrix} a \\ a \end{bmatrix} - \begin{bmatrix} b \\ c \end{bmatrix} = \begin{bmatrix} a-b \\ a-c \end{bmatrix} \quad \nabla_y I(a)$$

2 equations with **3 unknowns**,
need constraints



$$\otimes \begin{bmatrix} 1 & -1 \end{bmatrix}$$

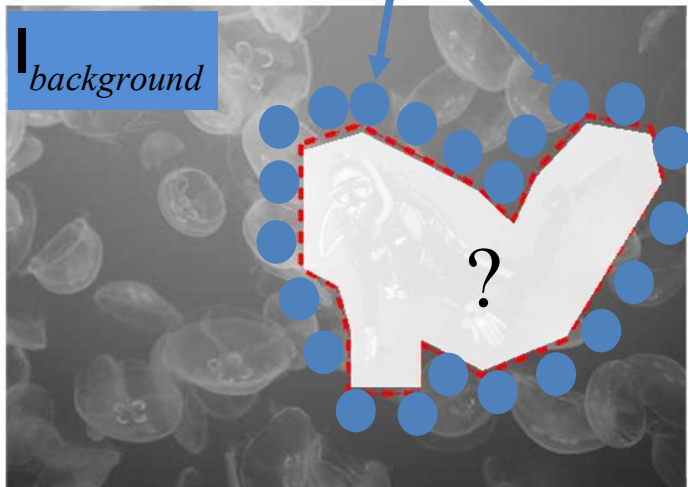
$$\otimes \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$



eg

$$\begin{bmatrix} a & - & b \\ a & - & c \end{bmatrix} = \begin{bmatrix} \text{gray} \\ \text{gray} \end{bmatrix} \begin{bmatrix} \nabla_x I(a) \\ \nabla_y I(a) \end{bmatrix}$$

Boundary condition

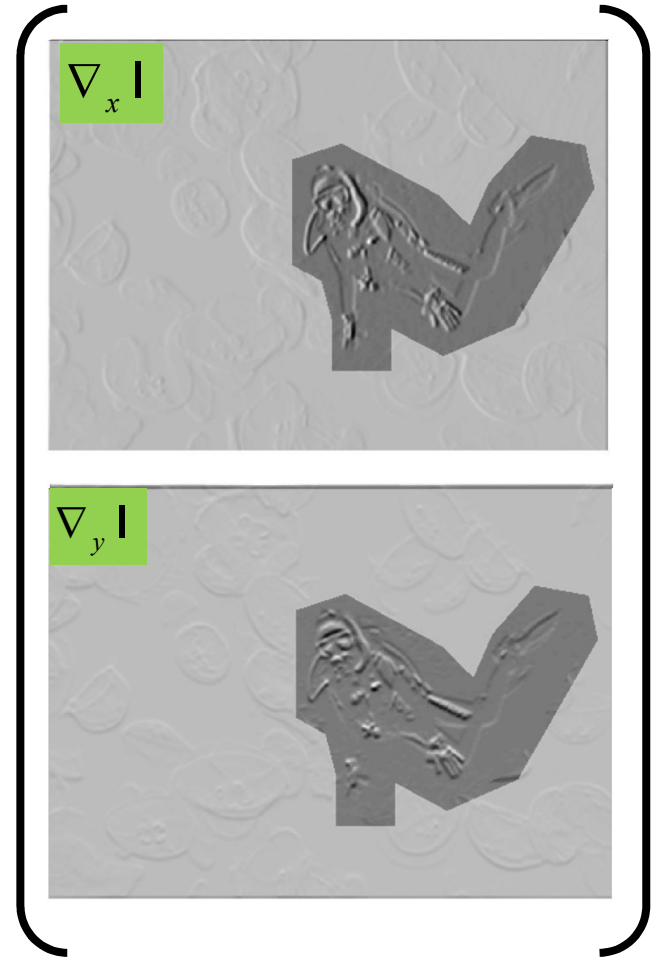


$$\begin{bmatrix} 1 & -1 \end{bmatrix}$$

=

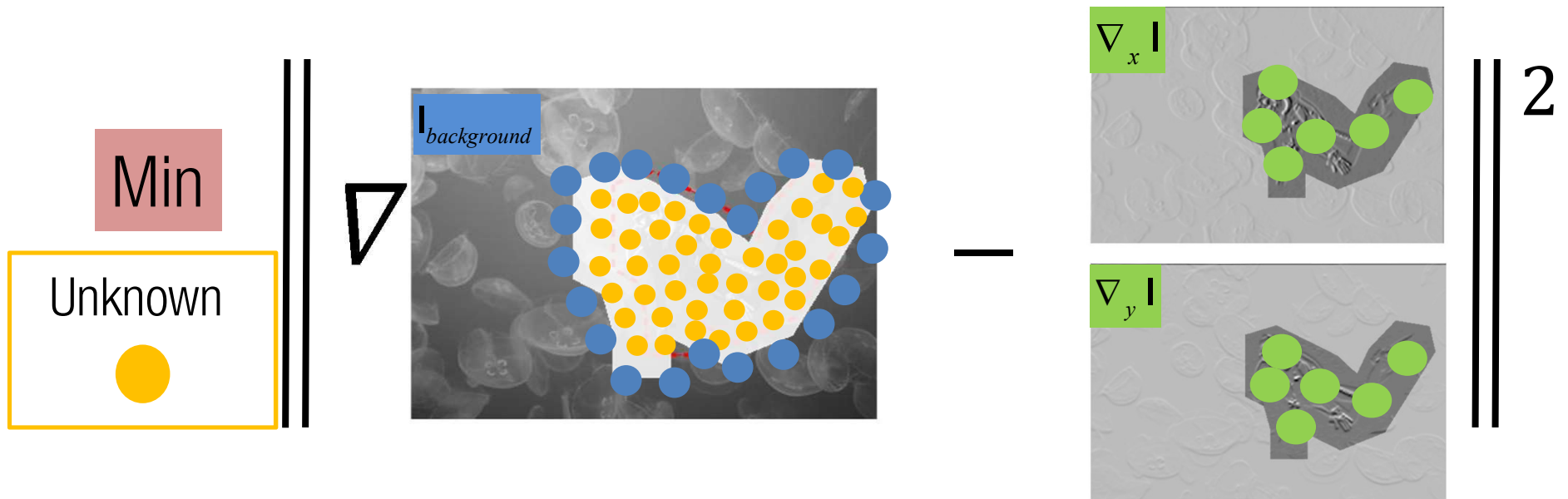


$$\begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

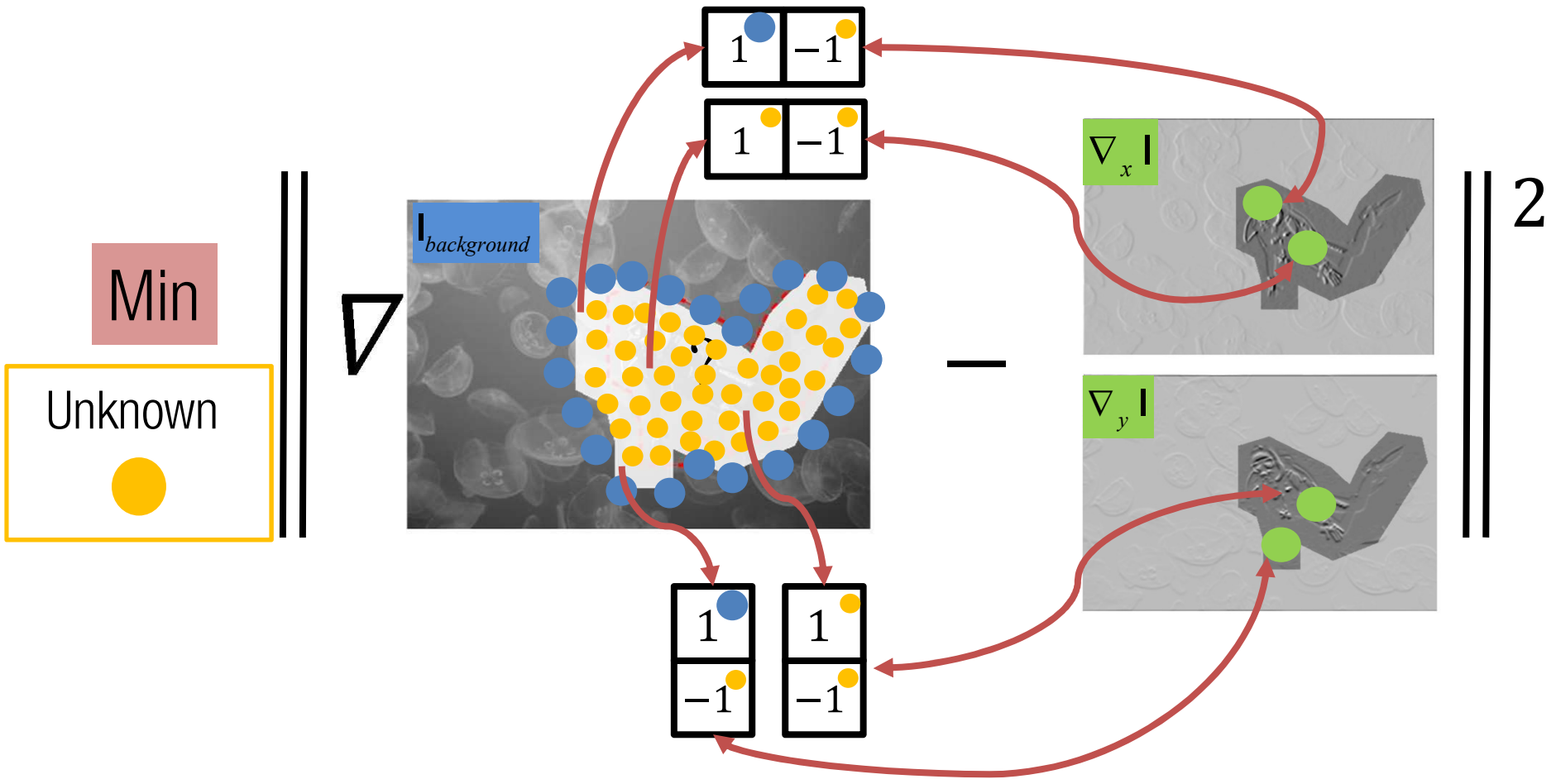


- Keep the value on boundary $\partial\Omega$ the same

Least Square Problem

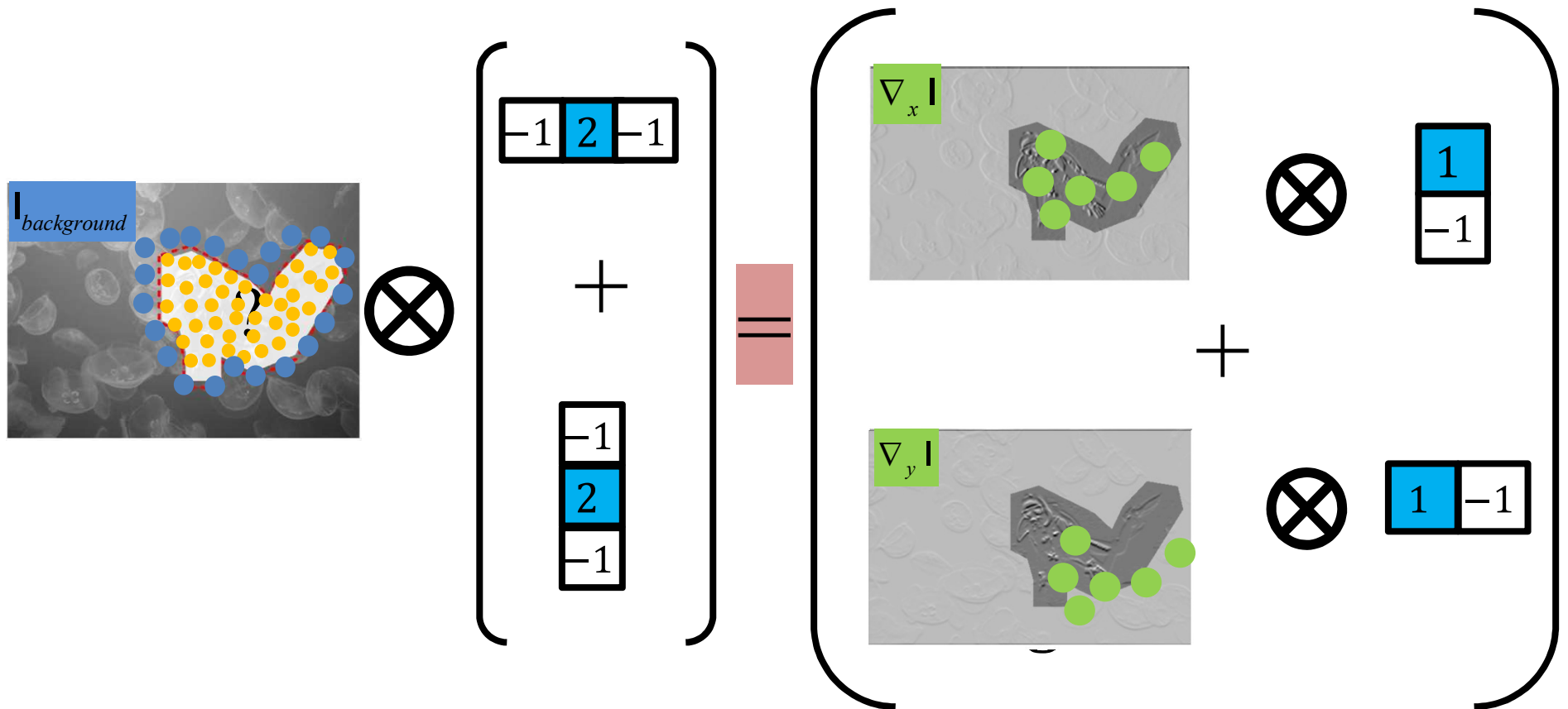


- Minimize the loss with respect to all pixels in the region Ω
- Keep the boundary $\partial\Omega$ the same

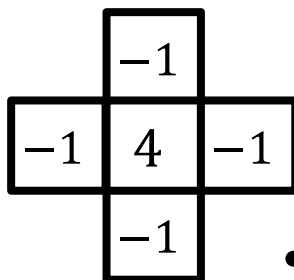
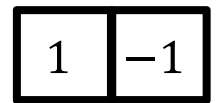
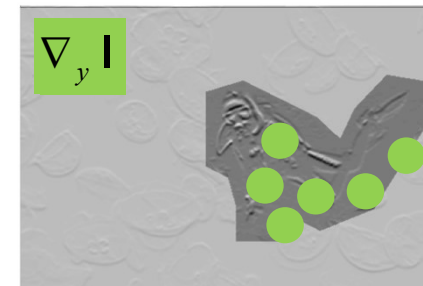
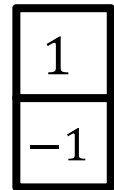
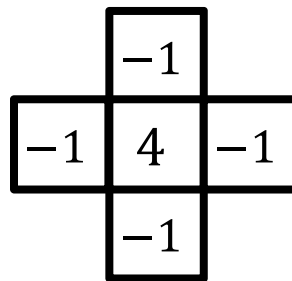
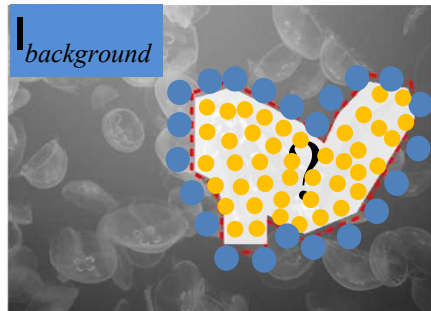
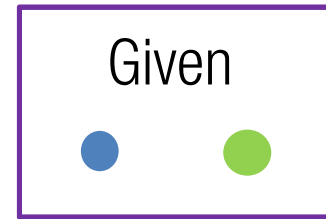


2

Least square solution



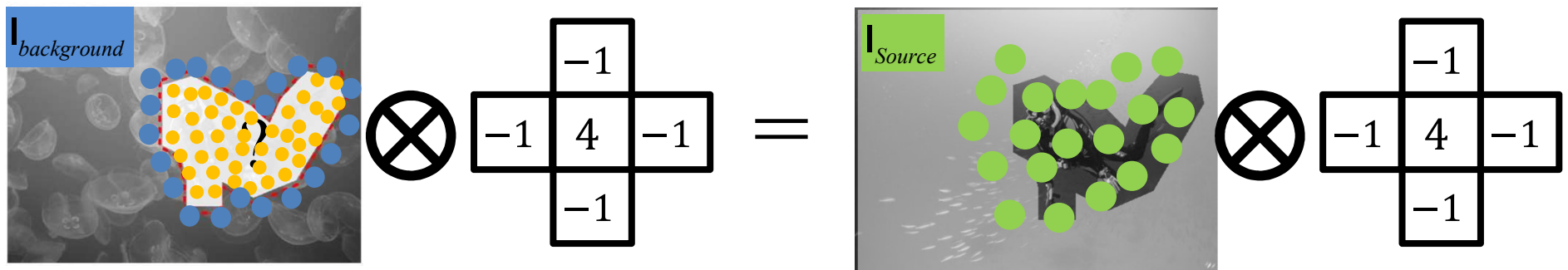
Solution on Pixels



- The convolutional kernel for Laplacian operator

Special case

- When the $\begin{matrix} \nabla_x I \\ \nabla_y I \end{matrix}$ are directly computed from an image I_{Source} (without editing)



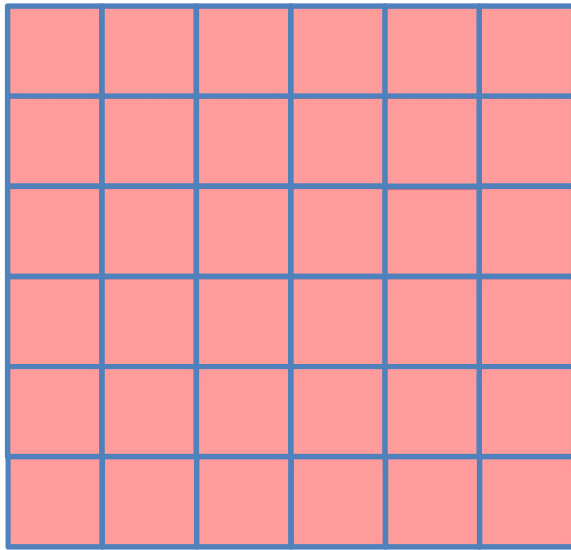
- Keep the value on the boundary $\partial\Omega$ the same
- Solve the equation for each channel (RGB) separately
- There is one equation matching the Laplacian values from the source to the target

Gradient Blending

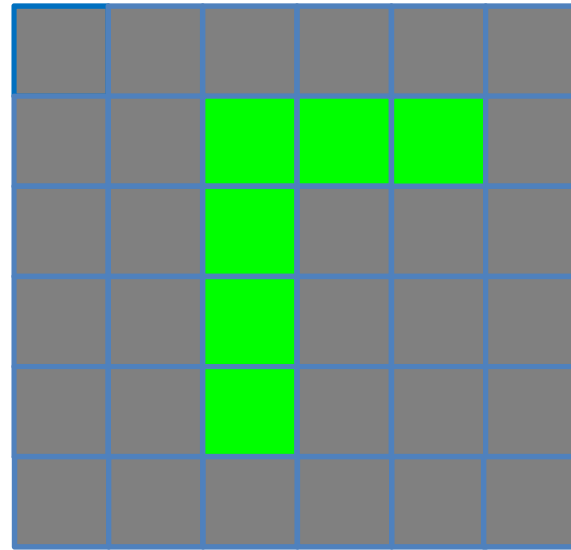


**How to solve this inverse
Laplacian problem ?**

An example



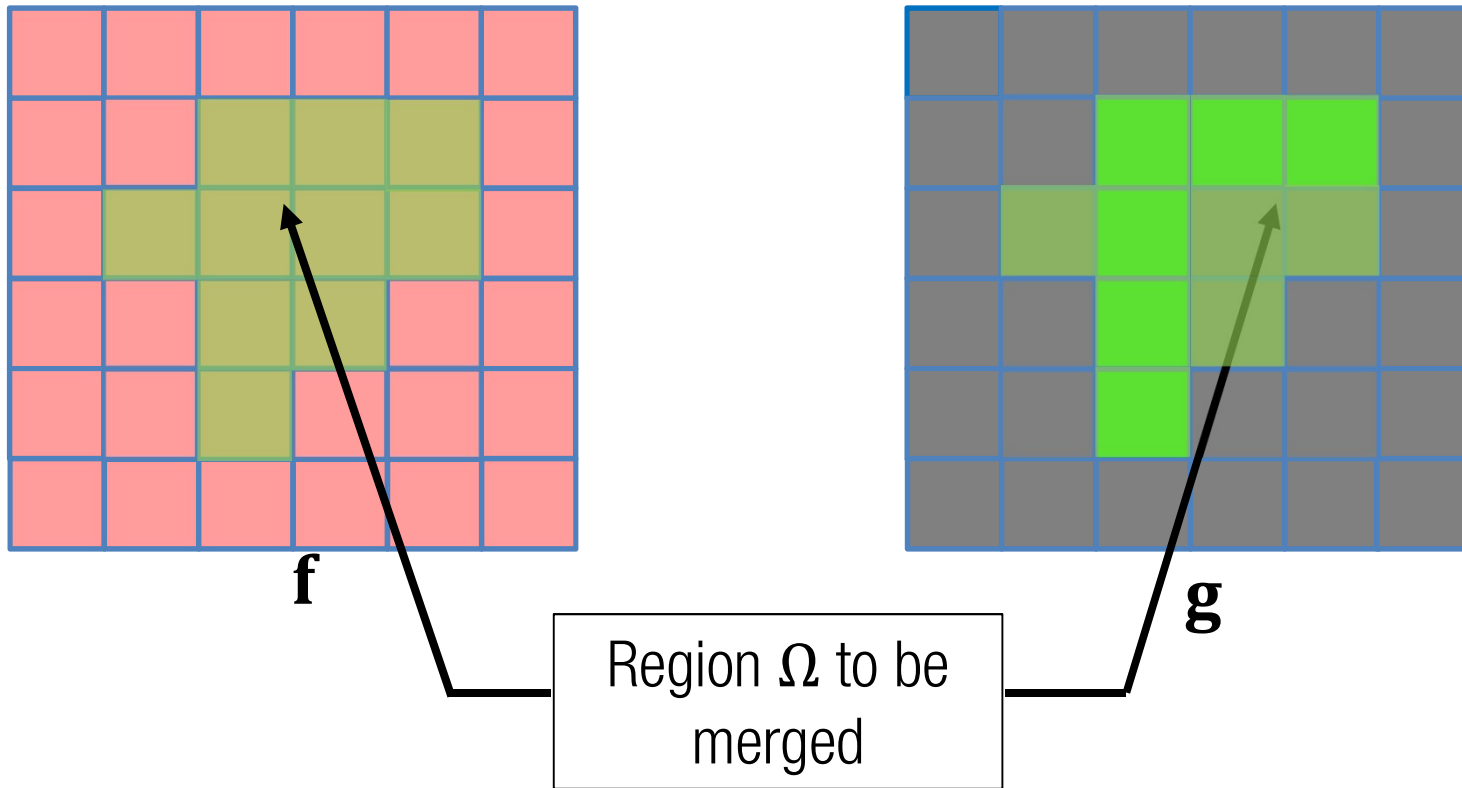
f



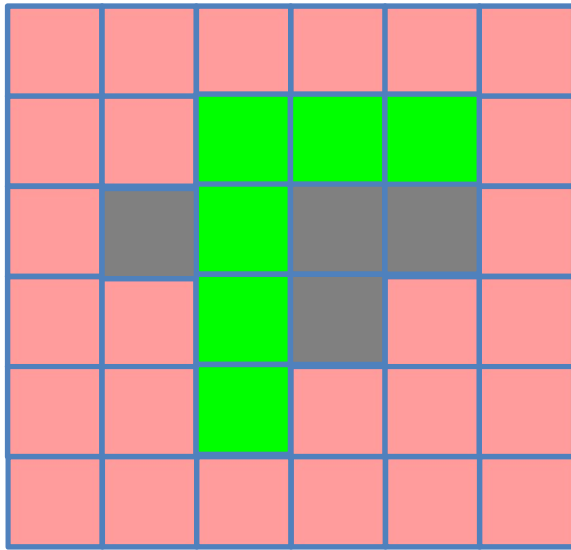
g

For the purpose of displaying, we use alpha mask for f and the background of g
The RGB value for f is (255,0,0), for the background of g is (0,0,0)

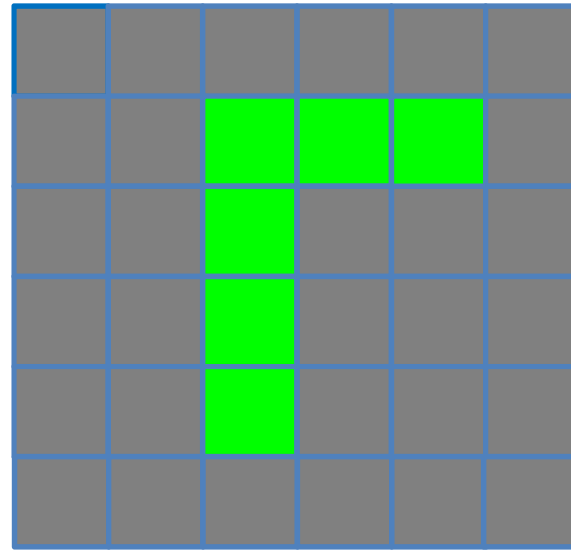
Mask for merging



Direct copy and paste

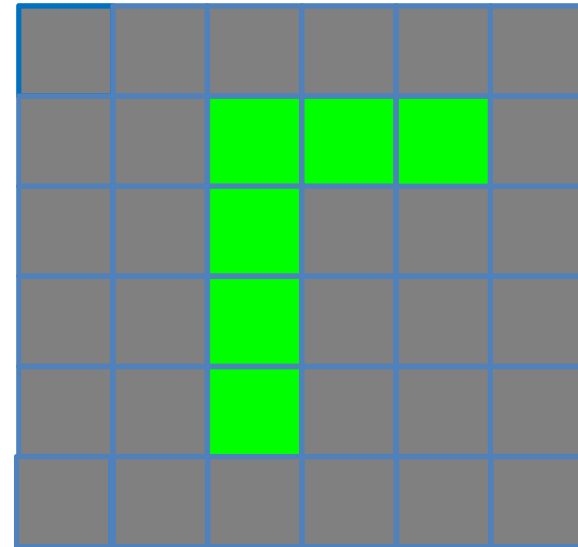
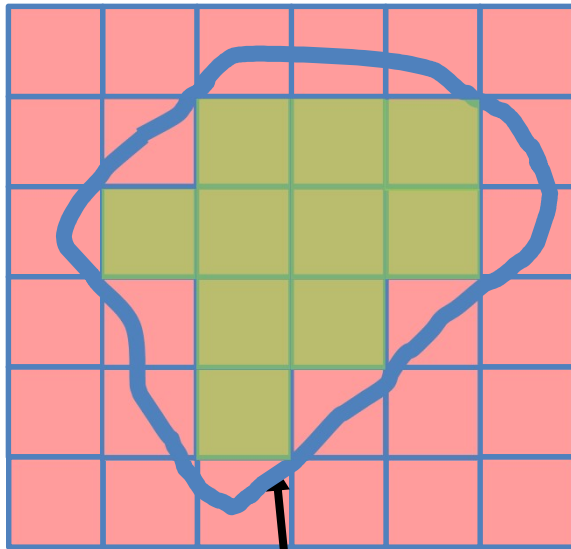


f



g

Keeping f the same on the boundary



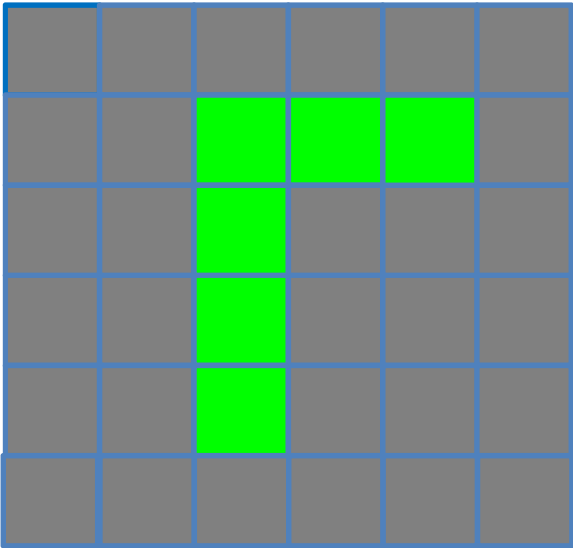
f

Region boundary $\partial\Omega$

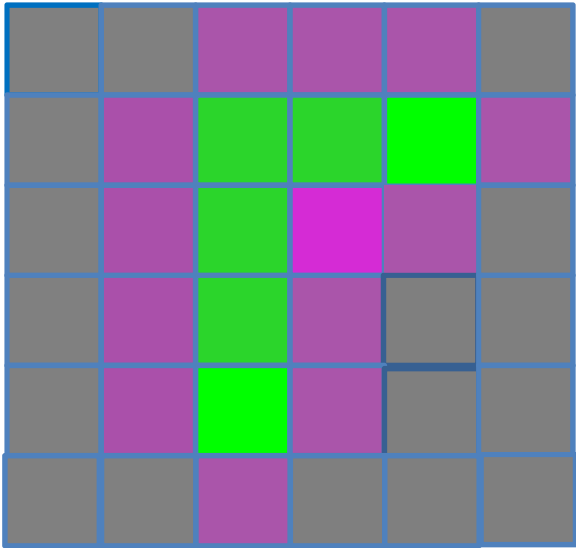
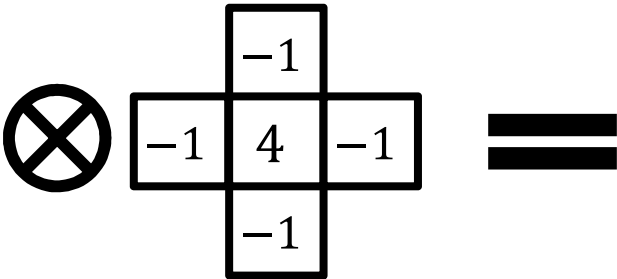
g

Keep f the same on the boundary $\partial\Omega$

Laplacian of the source

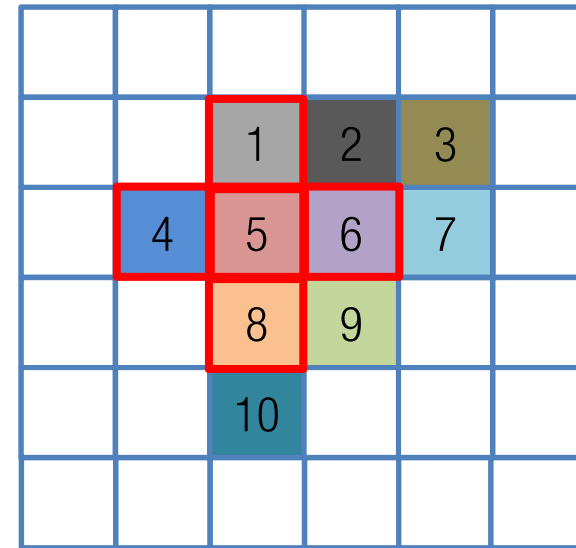


g

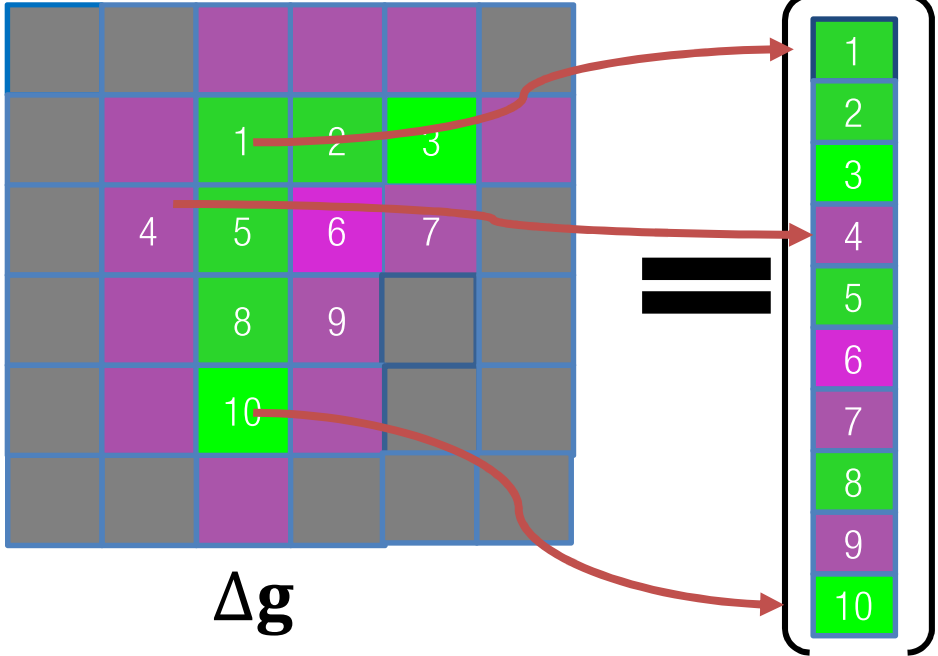
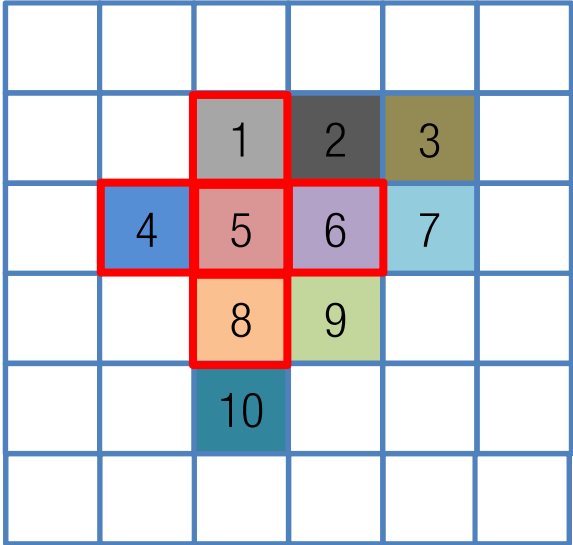


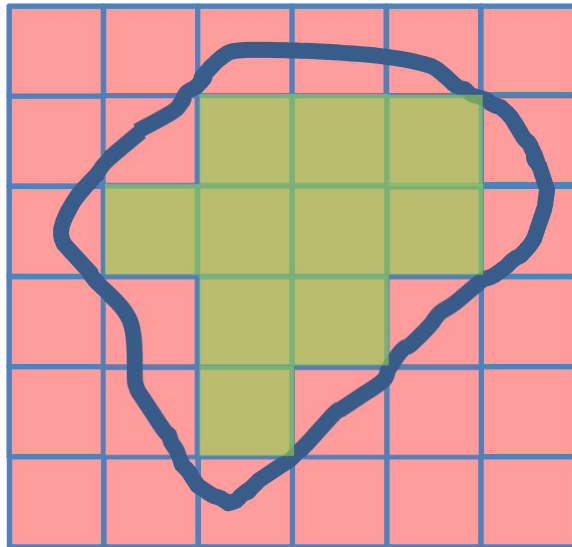
Δg

Before copying, we first index the pixels



Copying and *reshaping* the Laplacian of source





$$\begin{cases} \Delta \mathbf{f} = \mathbf{b} \text{ in } \Omega \\ \mathbf{f}|_{\partial\Omega} \text{ keeps same} \end{cases}$$

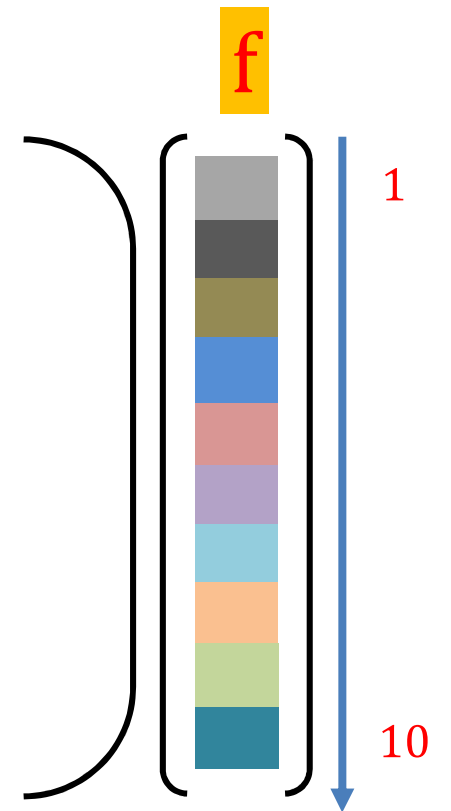
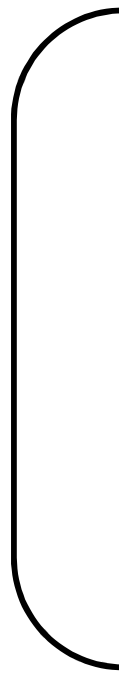
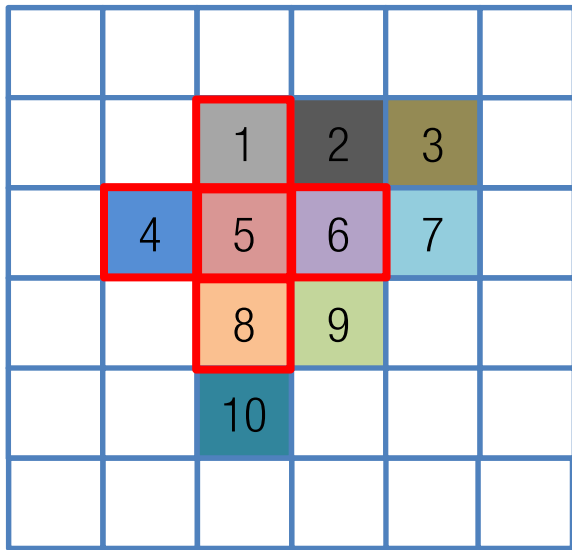
$$\Delta \mathbf{f} = \mathbf{b}$$

Δ is a linear operator...

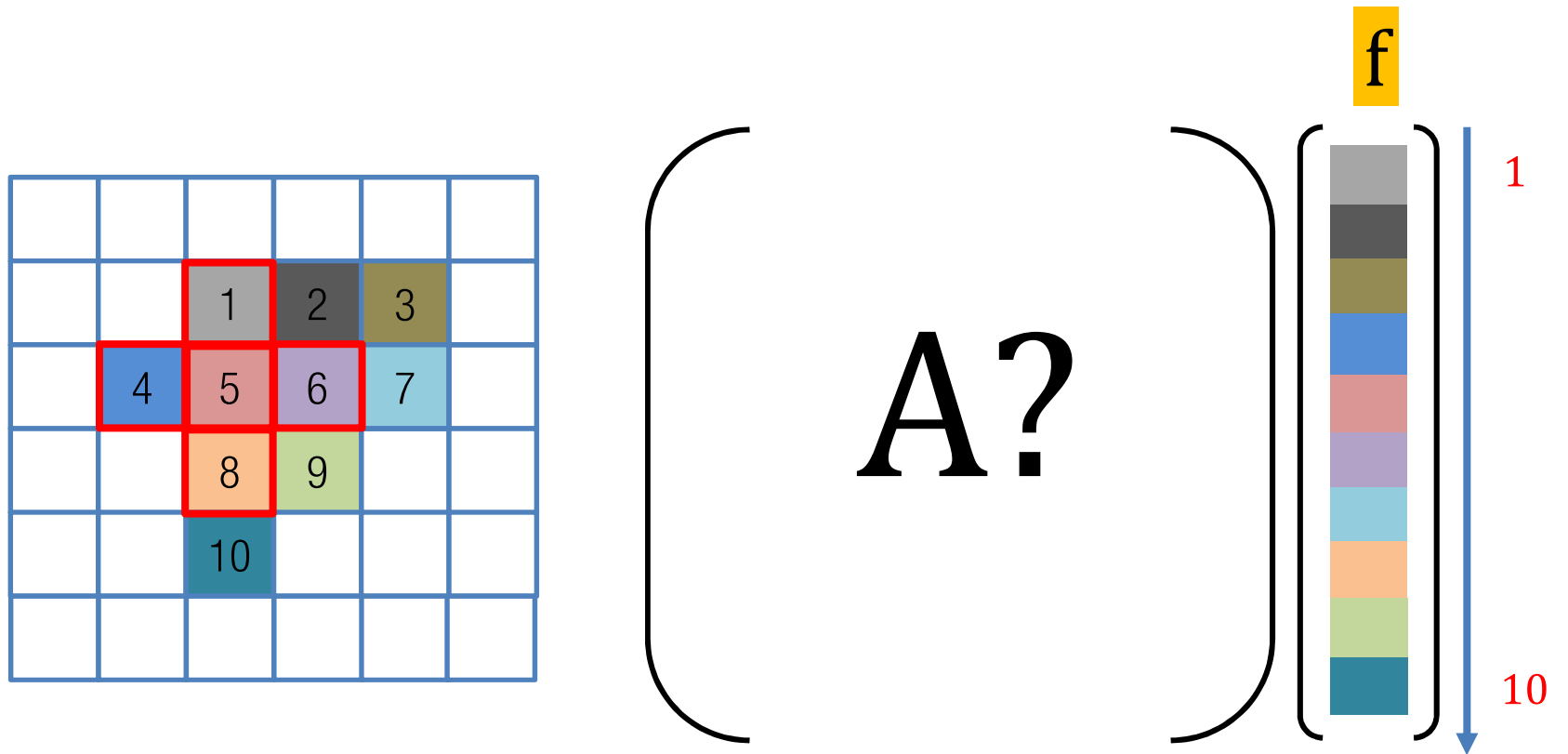
$$\mathbf{A}\mathbf{f} = \mathbf{b}$$

...We can use a matrix \mathbf{A} to encode it!

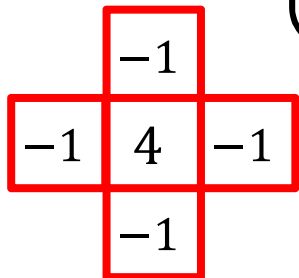
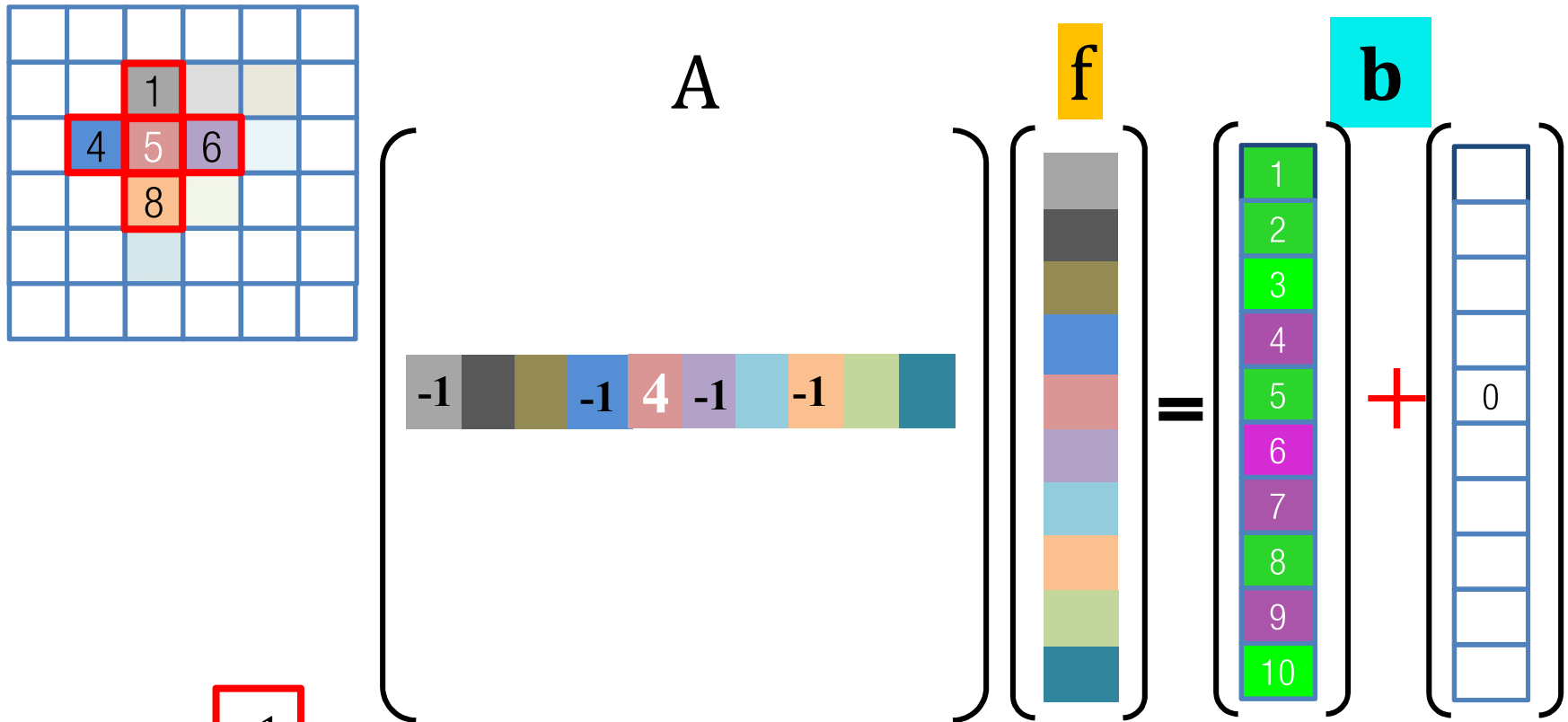
Indexing the unknowns



Laplacian as a matrix?

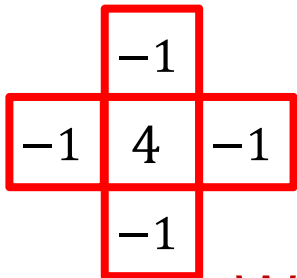
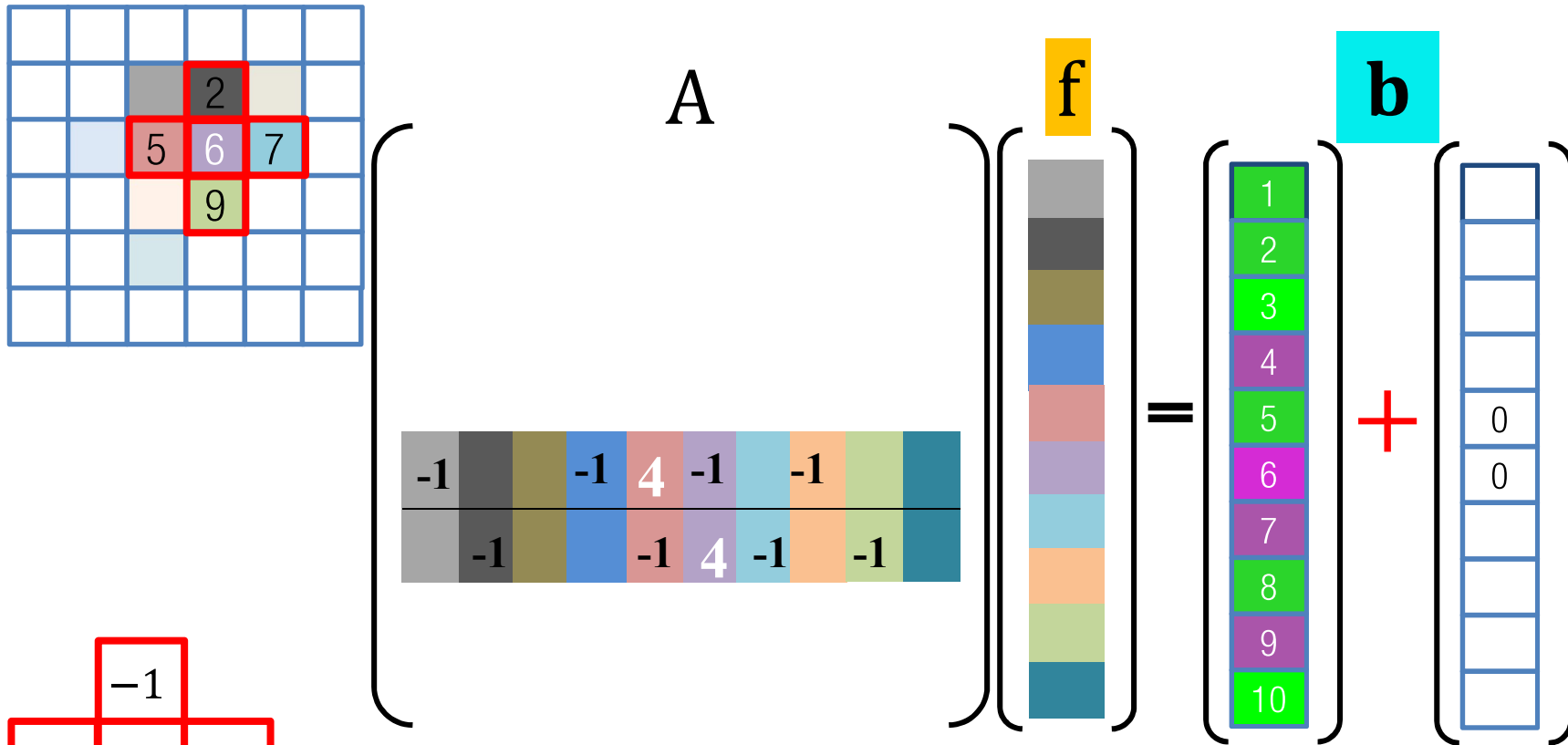


Matrix A encoding the Laplacian operator



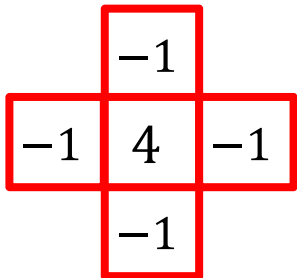
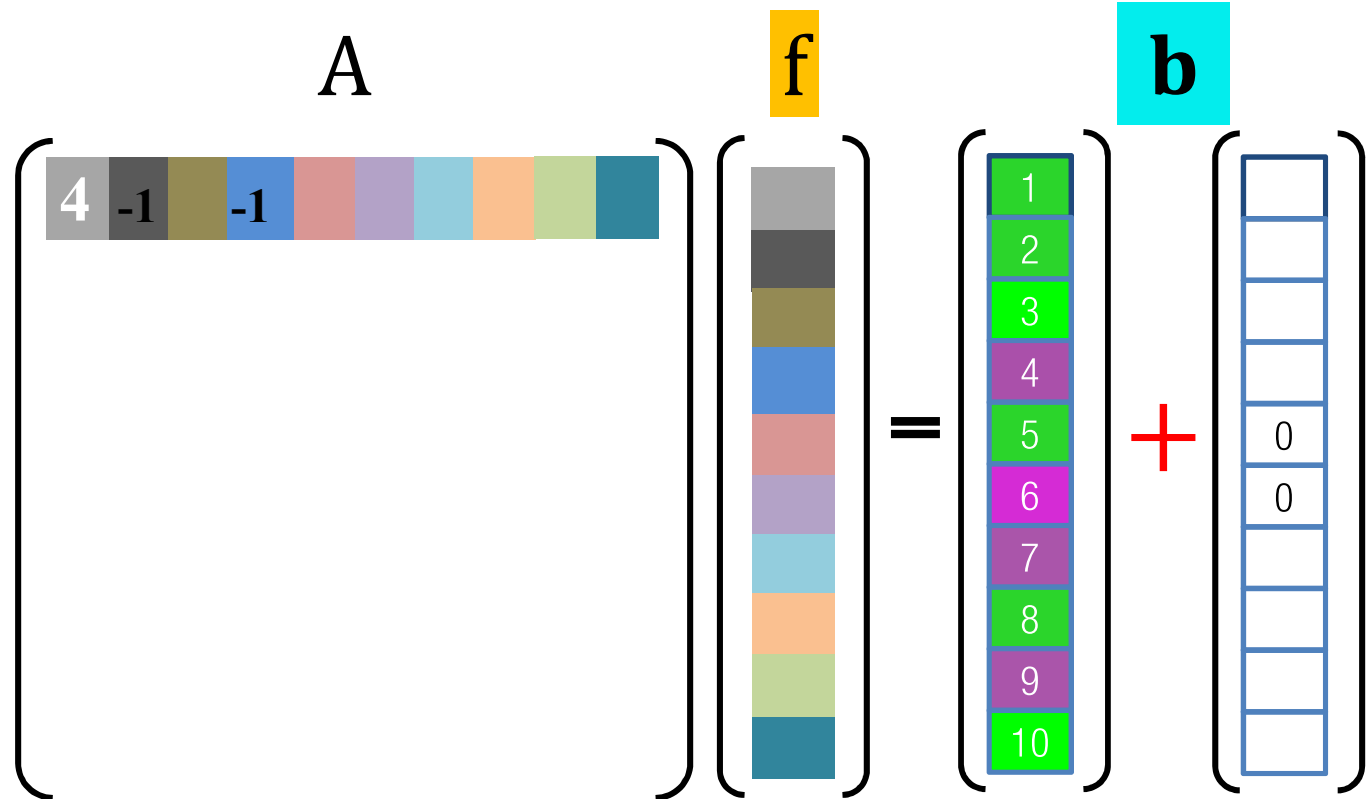
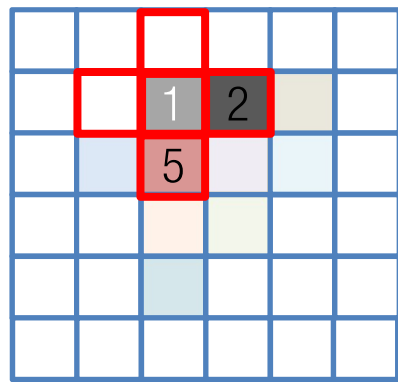
When the pixel is in the region

Matrix A encoding the Laplacian operator



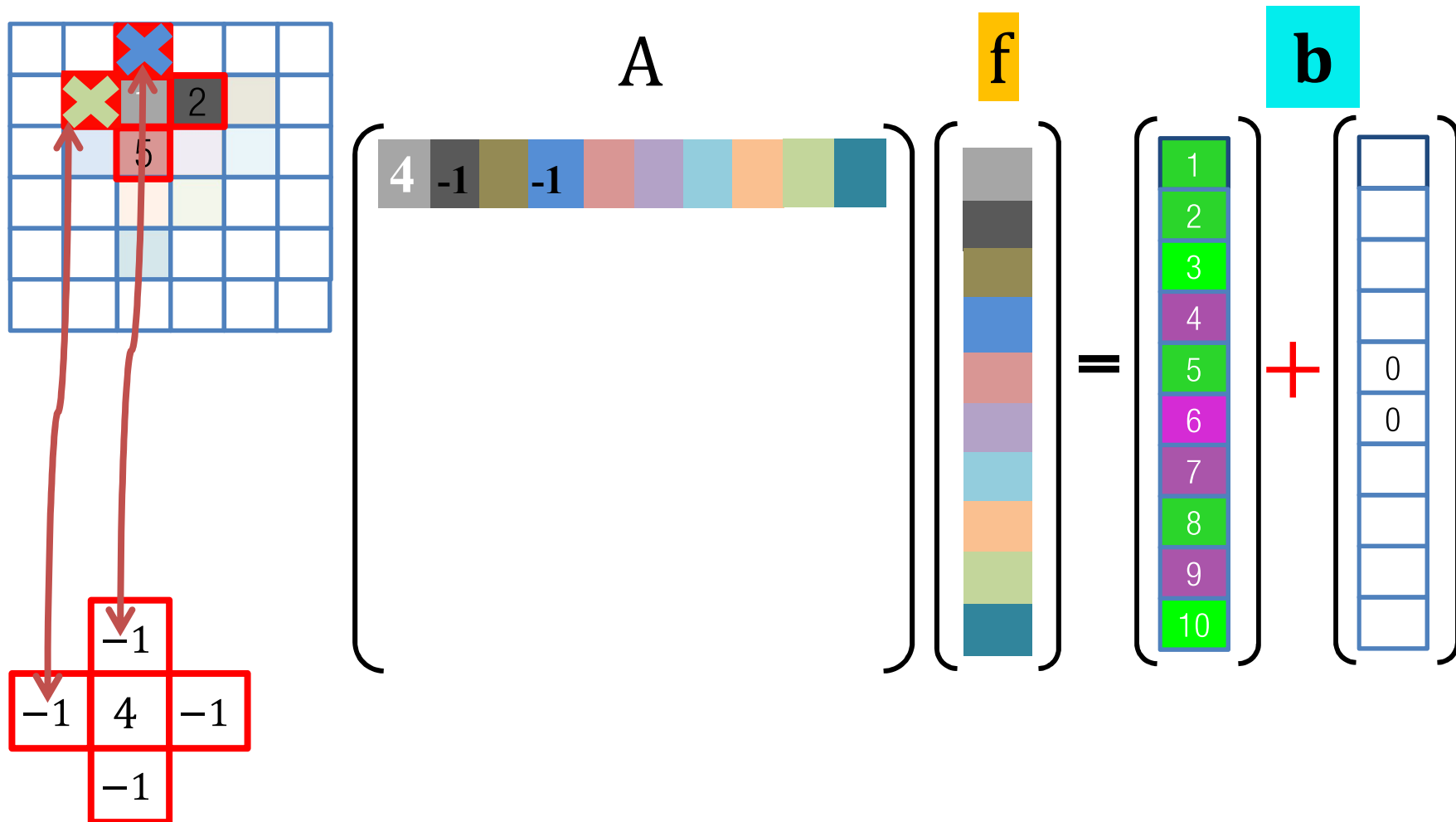
When the pixel is in the region

Matrix A : Laplacian operator

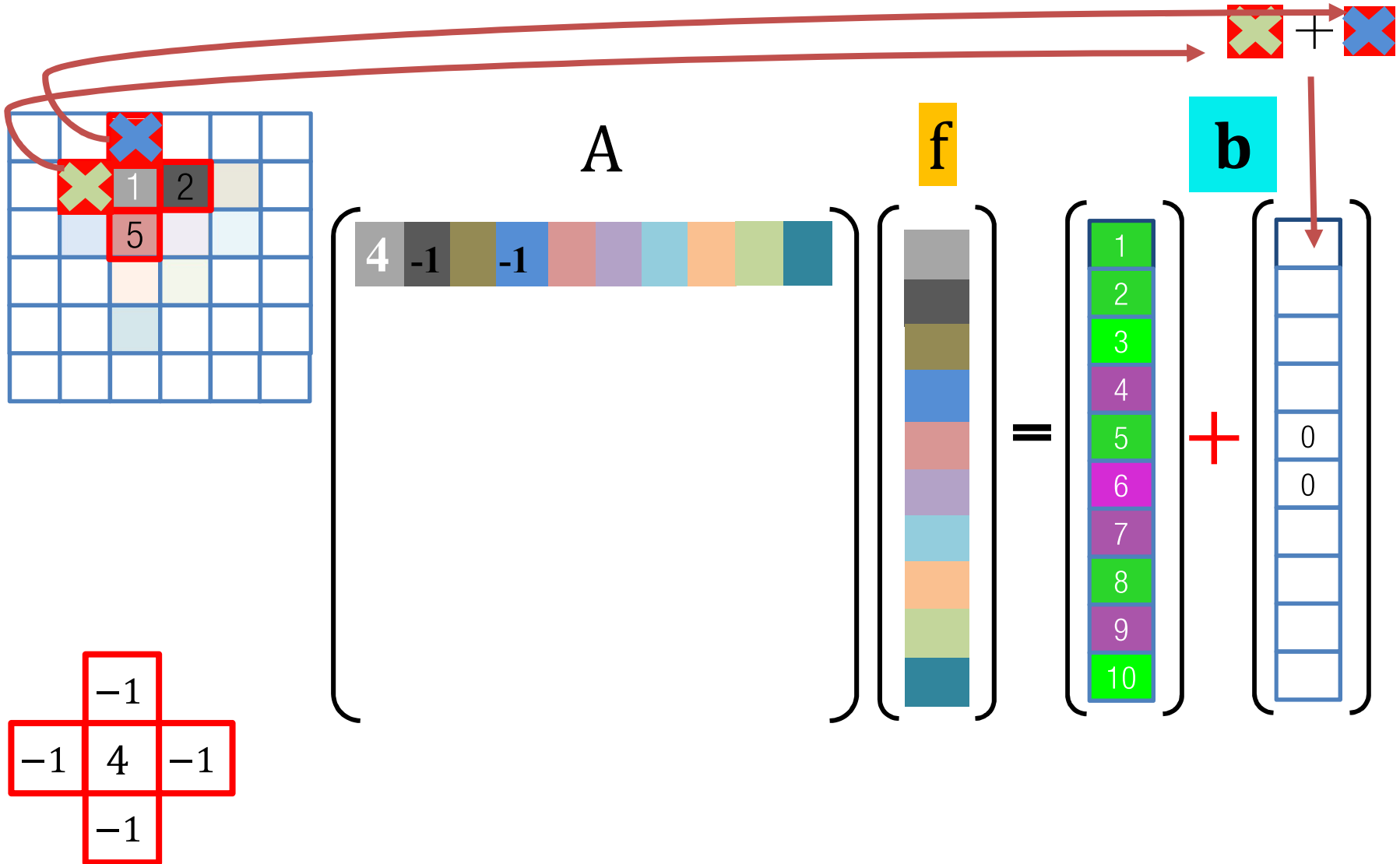


When the pixel is on the boundary

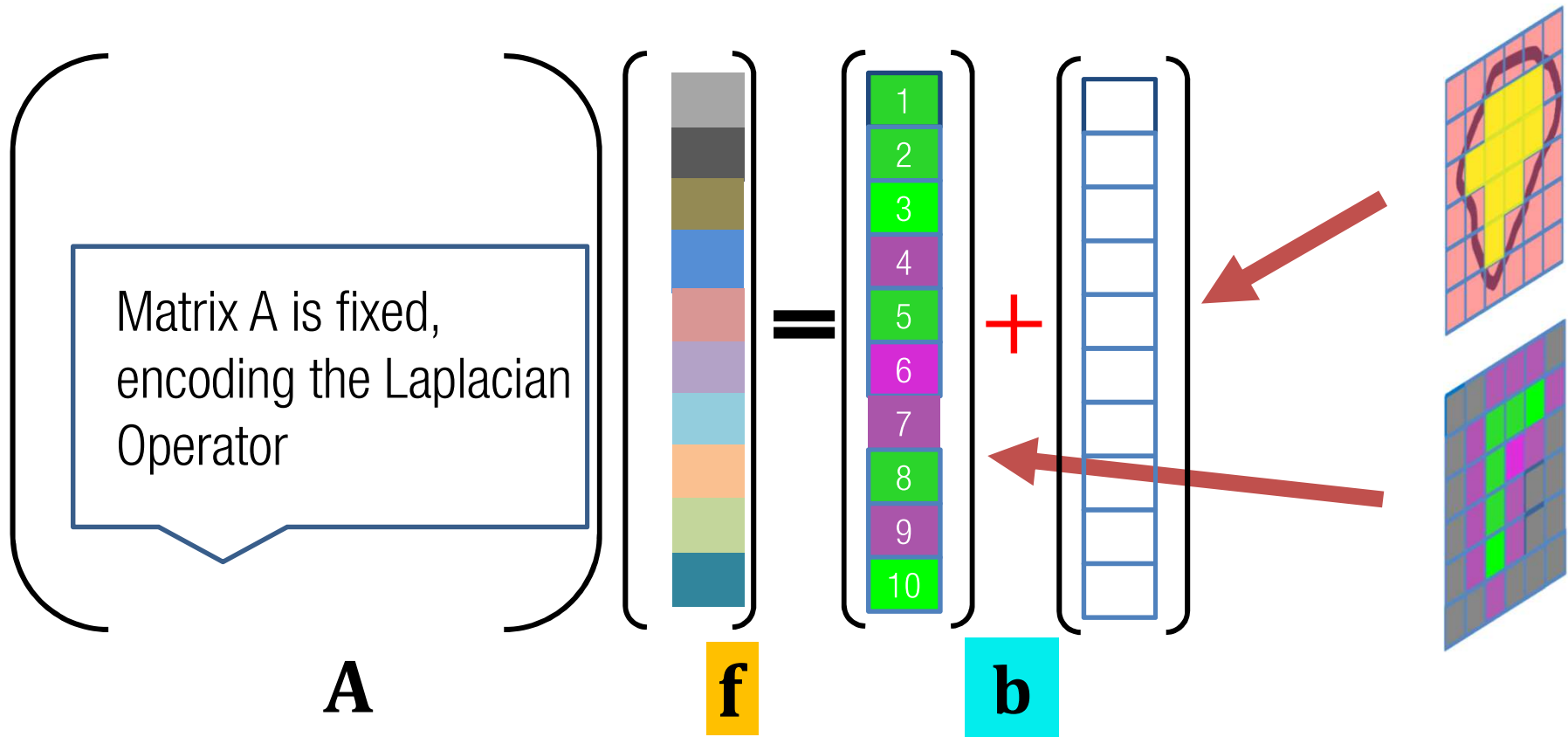
How to deal with the knowns Boundary Values?

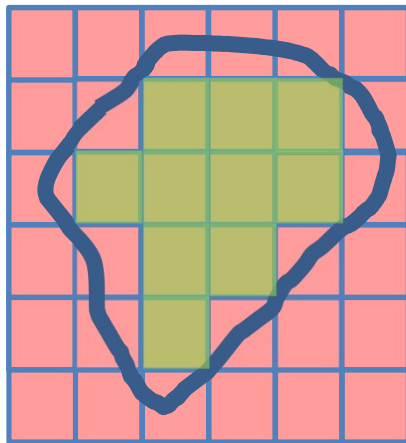
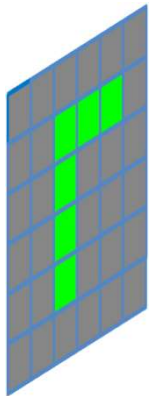
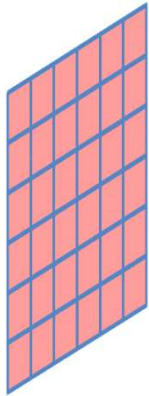


Move the boundary value of knowns to **b** side!

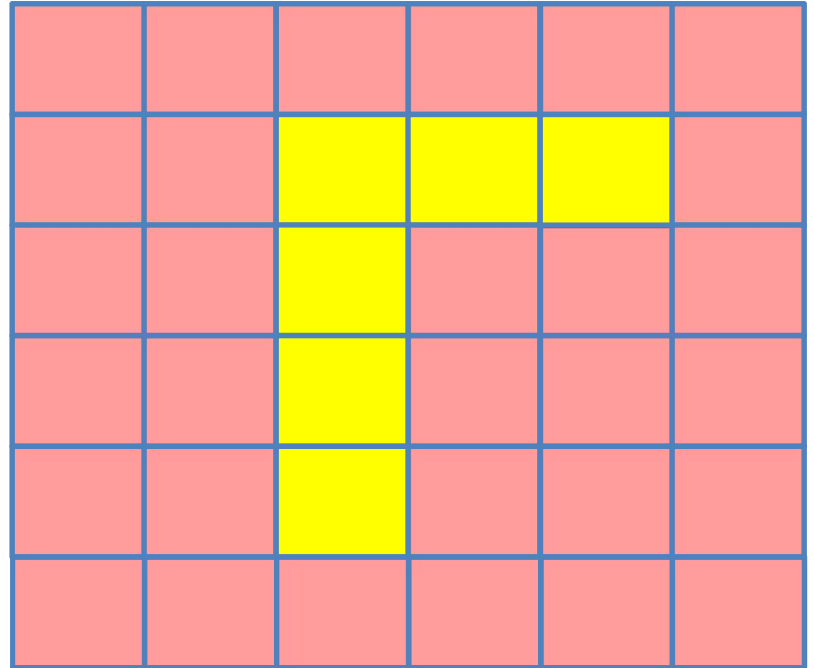
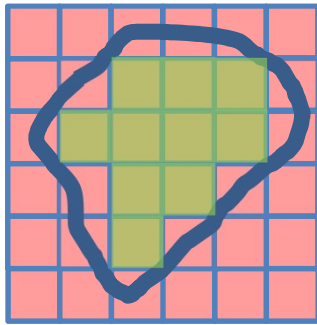
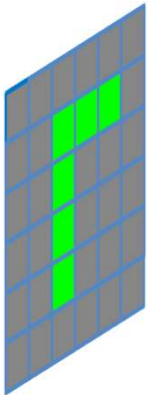
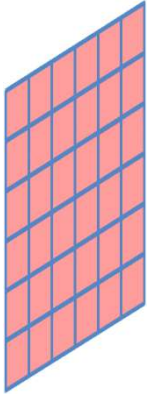


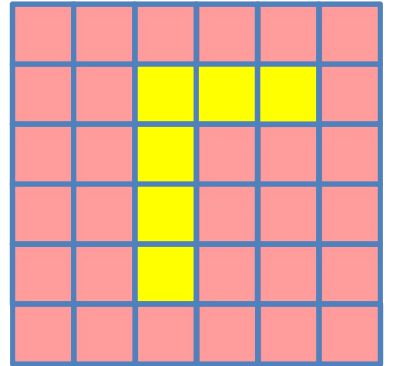
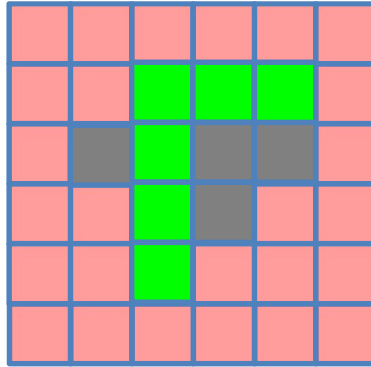
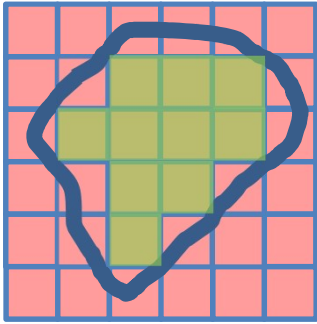
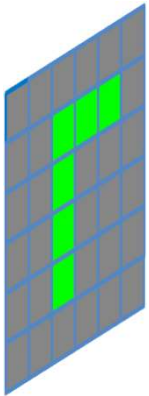
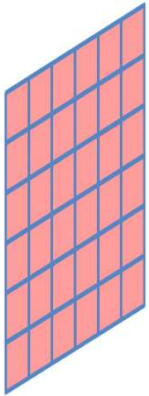
$$A\mathbf{f} = \mathbf{b}$$





Guess what's our blended image?

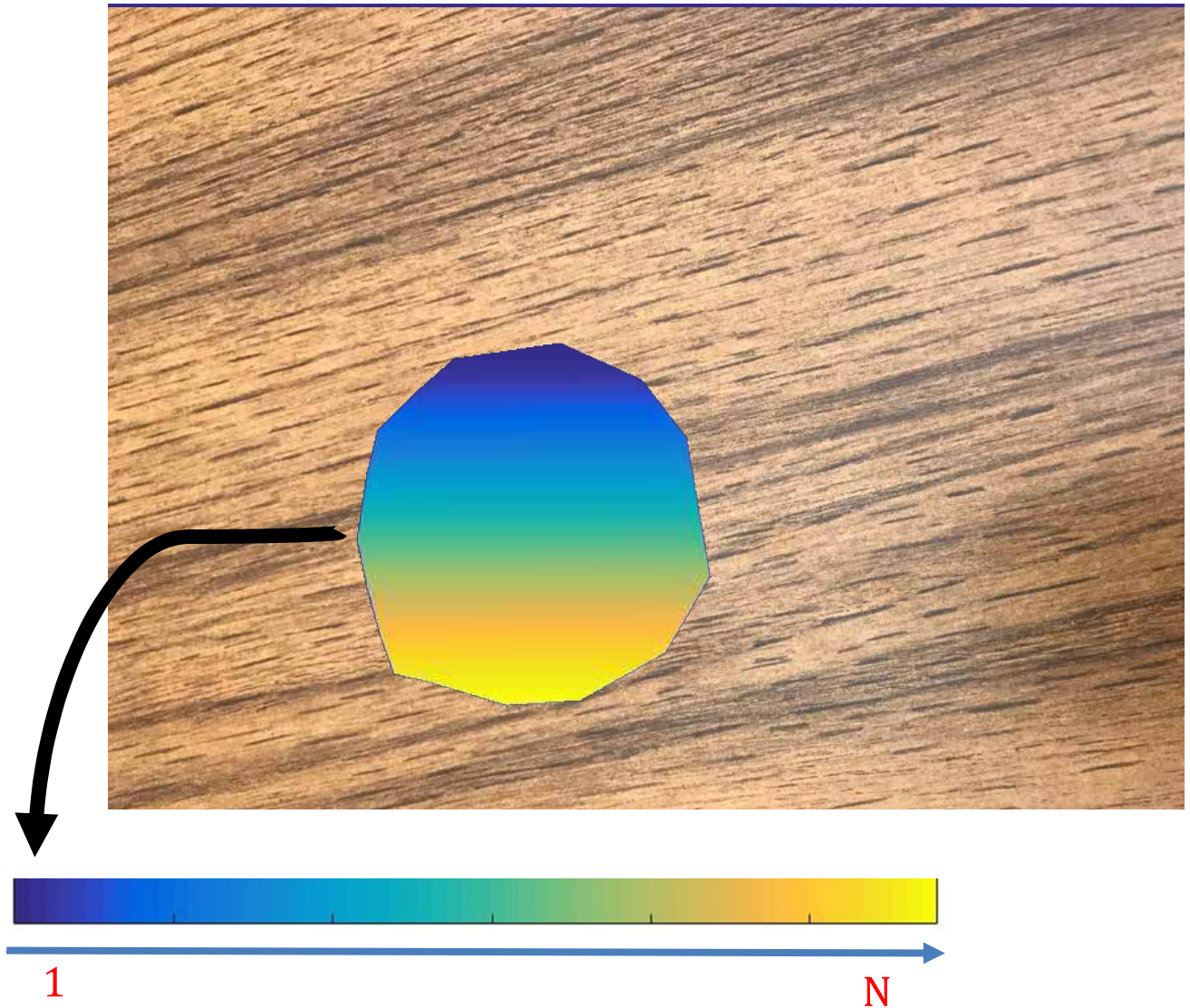




Let's summarize with a real image

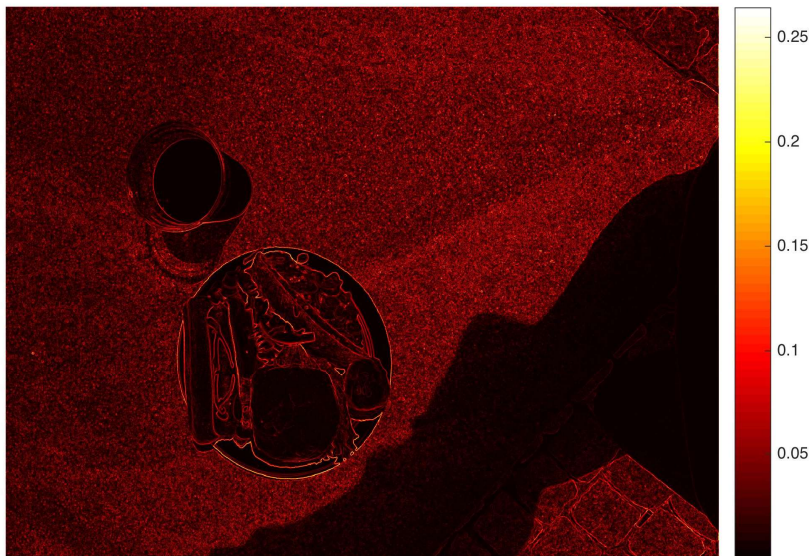


Step1. Indexing the unknowns in Target

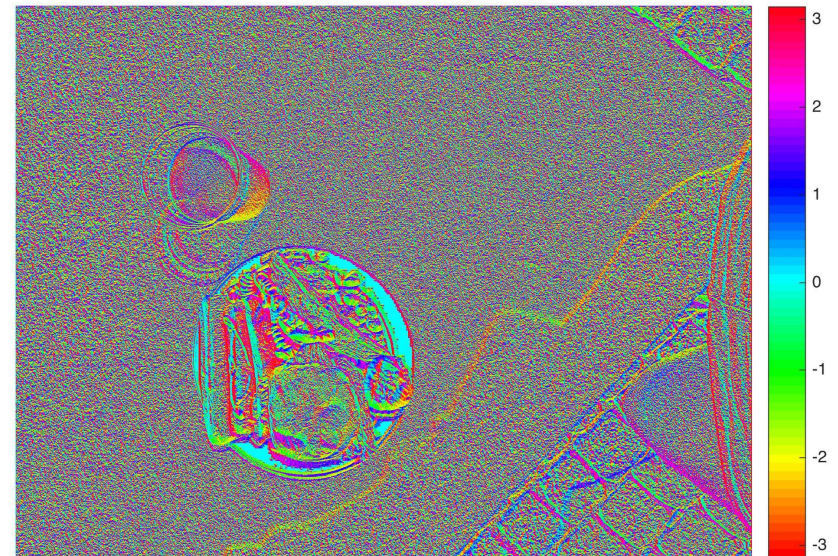


N is the number of unknowns

Step2. Copying the gradient from source

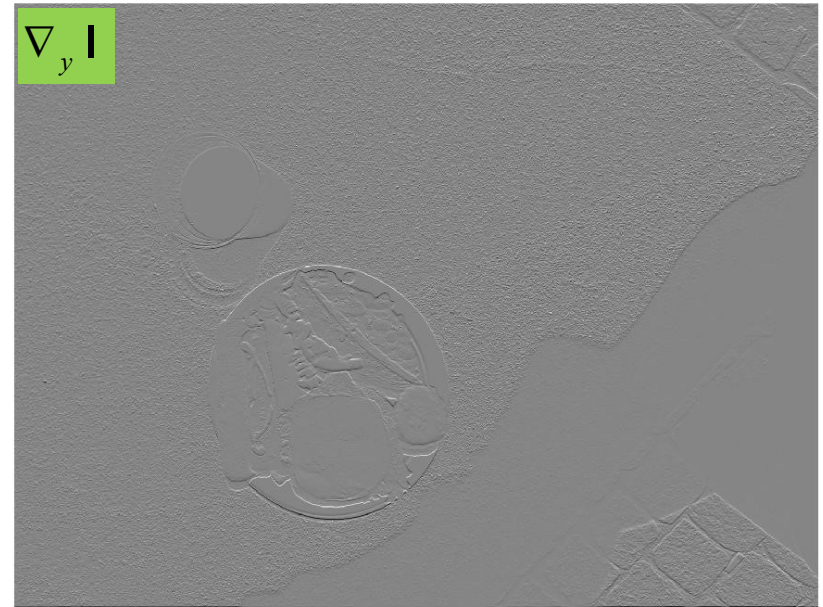
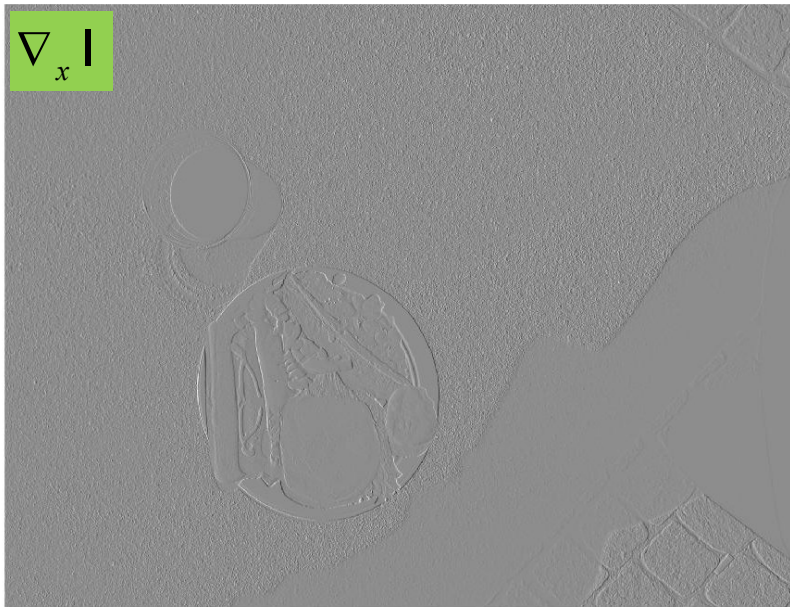


Gradient magnitude

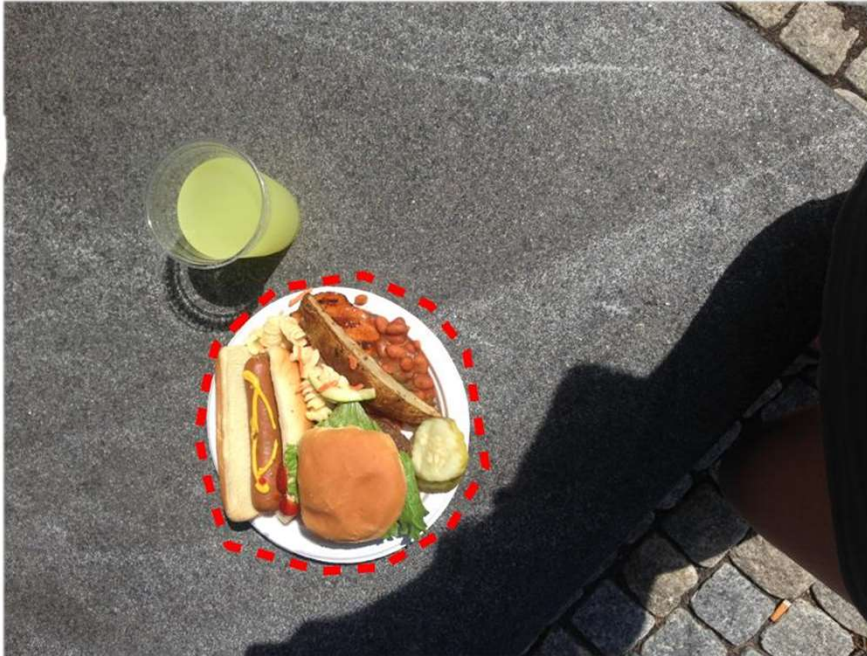


Gradient angle

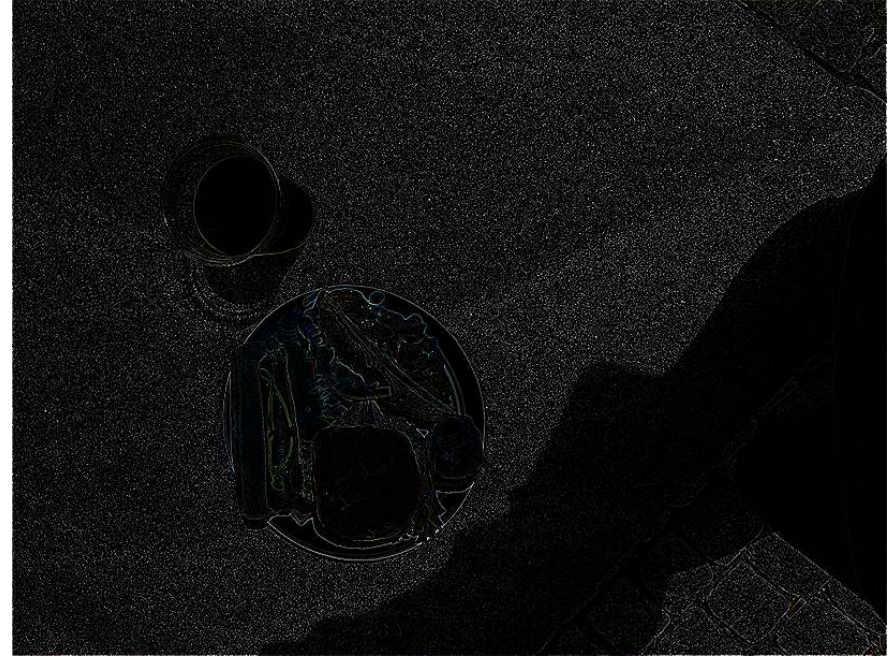
Step2. Copying the gradient from source



Step2. Compute the Laplacian from source

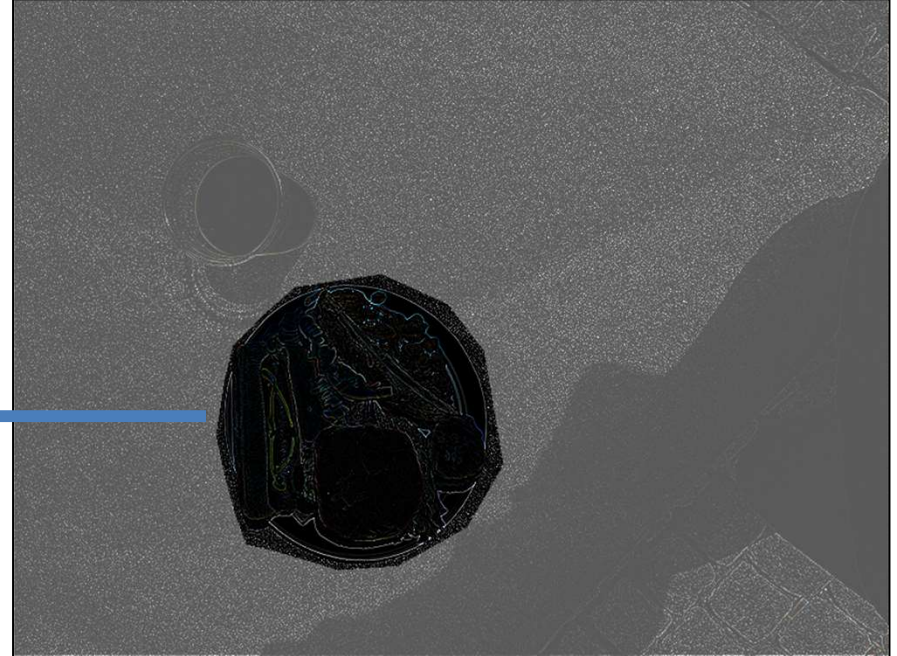
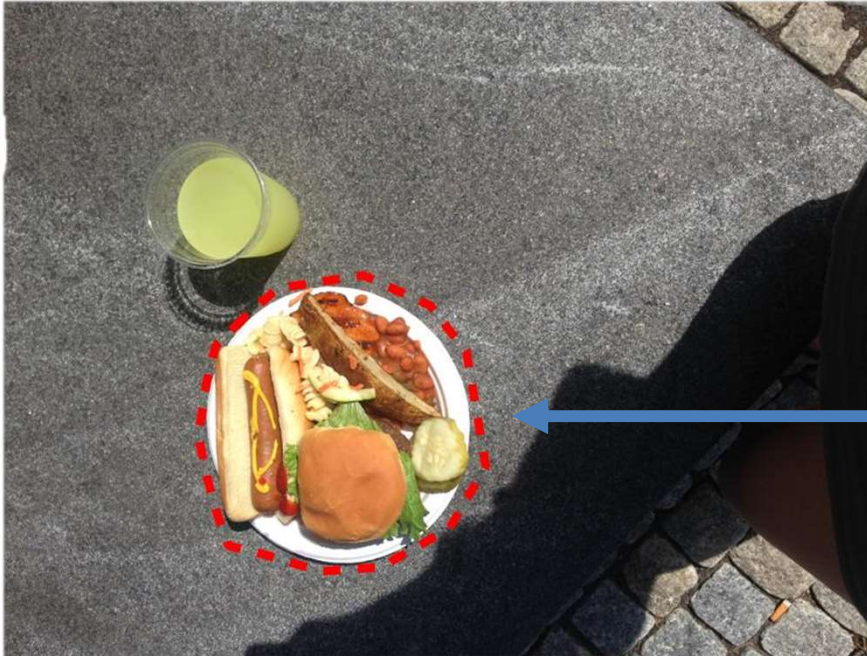


Source image



Laplacian

Step2. Copying the gradient from source

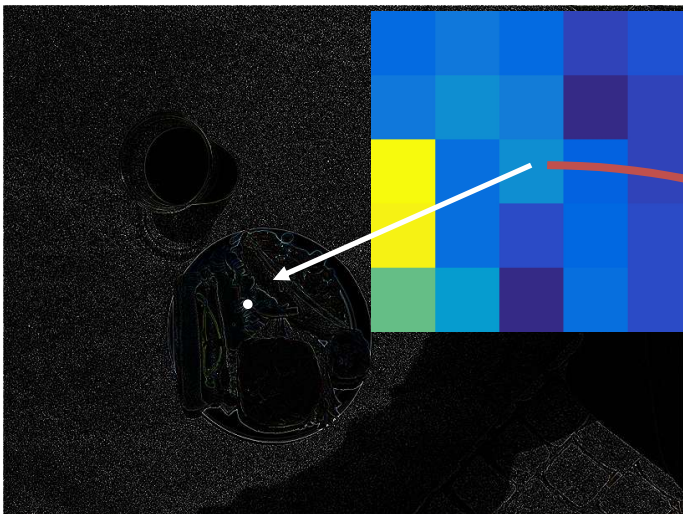
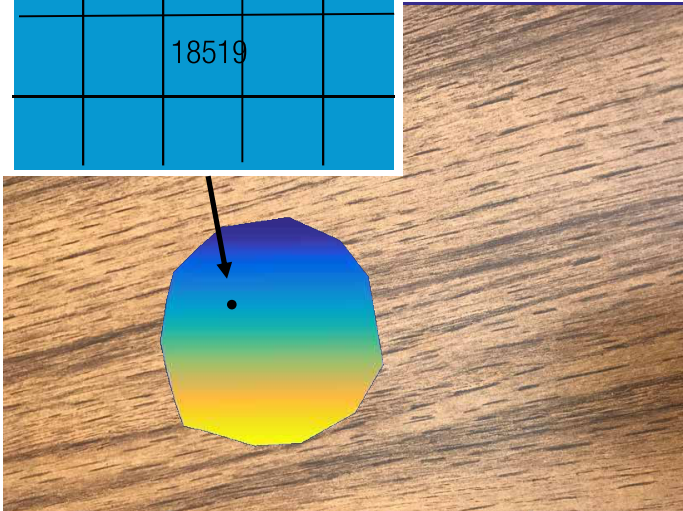


Step2. Cropping the masked Laplacian

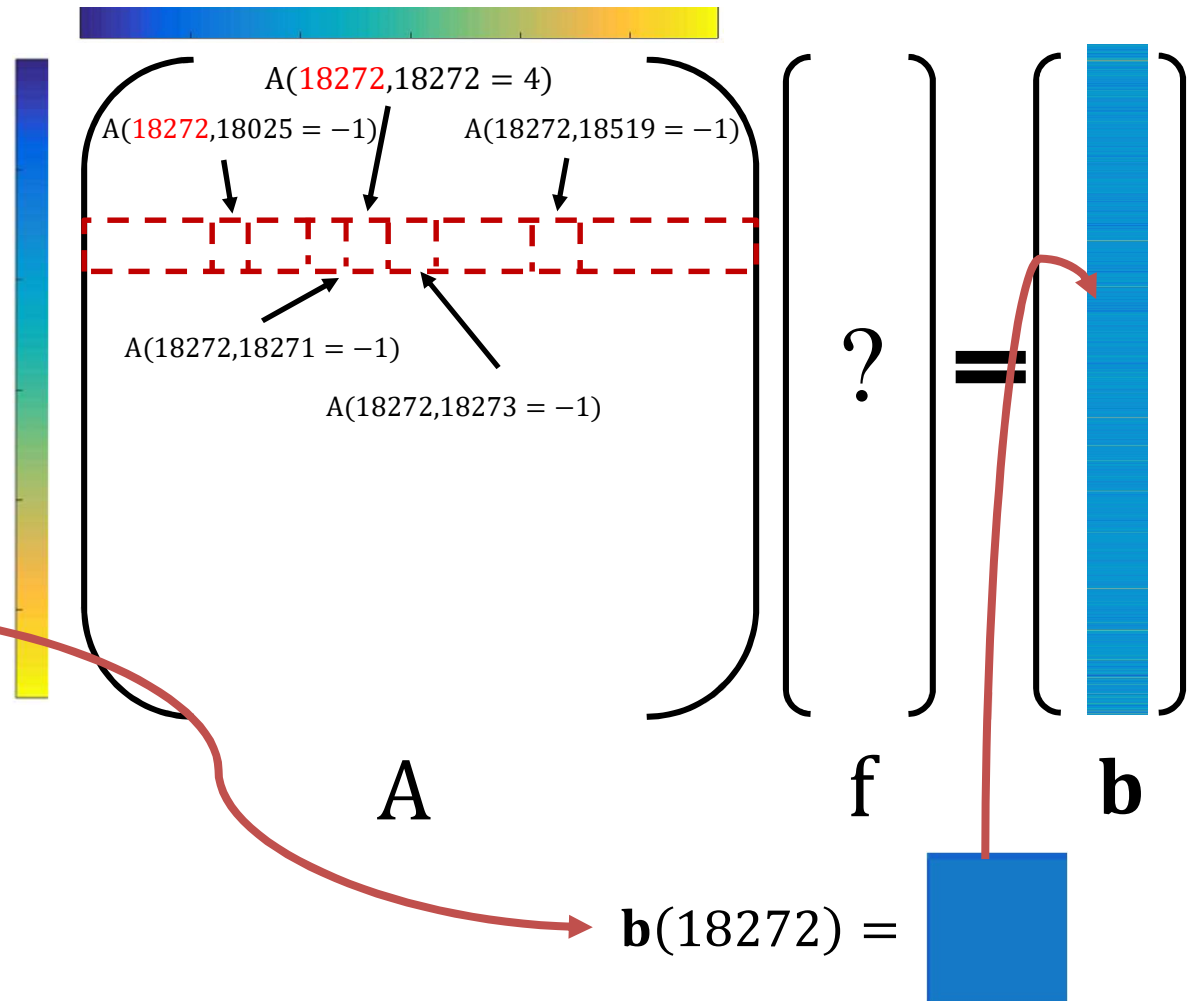


Step3. Constructing matrix A from the Laplacian operator

		18025		
18271	18272	18273		
		18519		

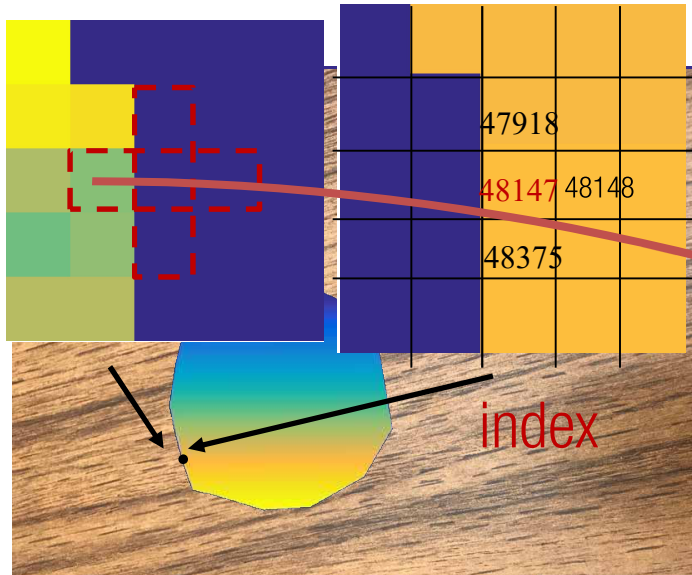


For pixel in the region

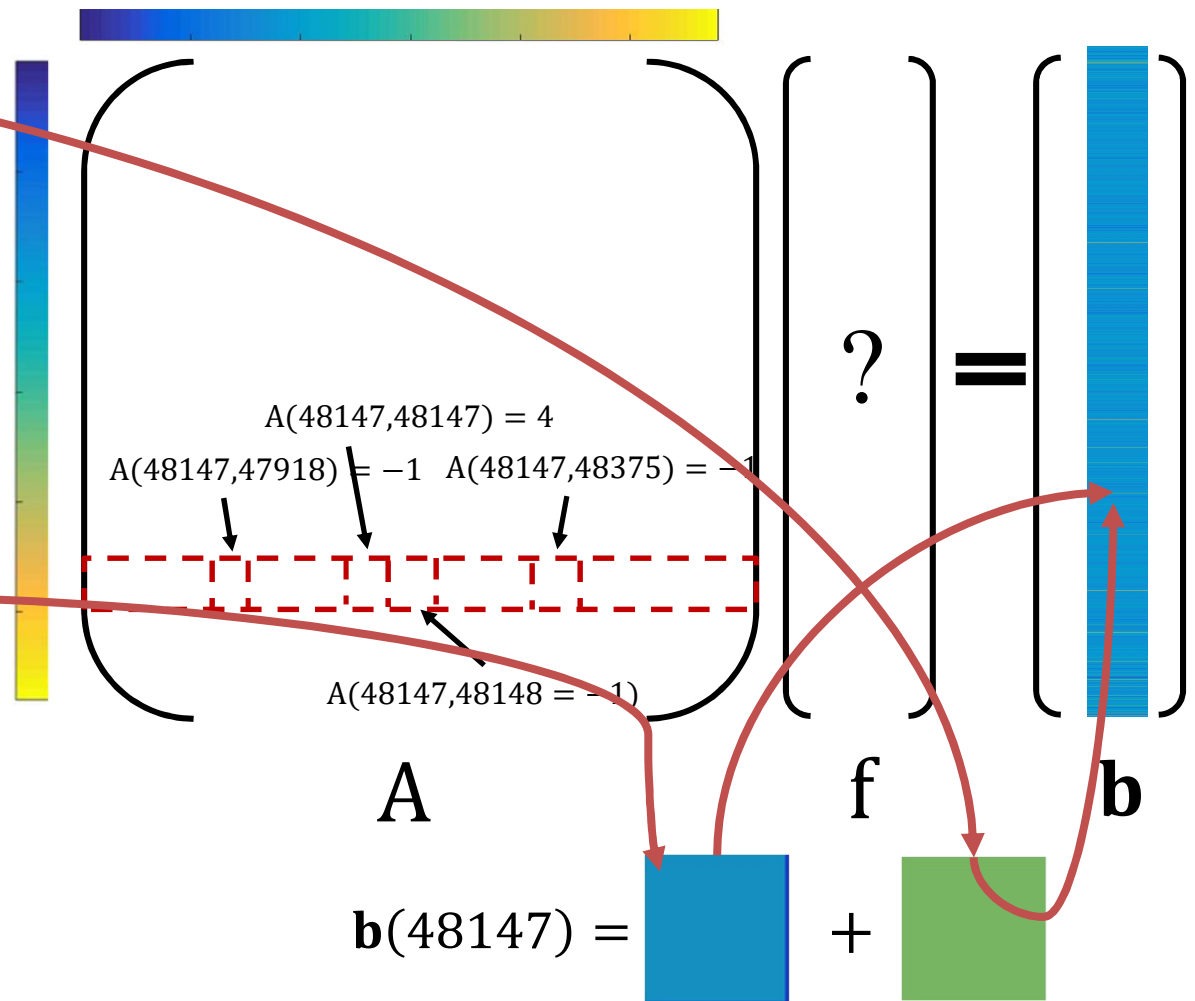
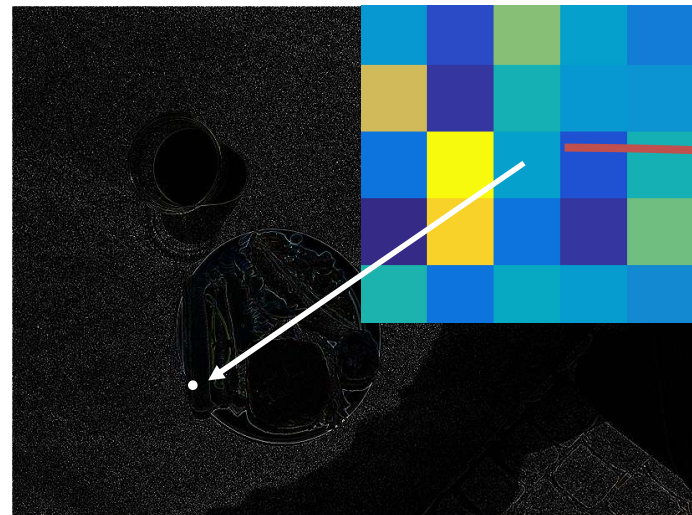


Step3. Constructing matrix A from the Laplacian operator

boundary value



For pixel on the boundary



Step4. Solving the linear equation and copy the values back to target







Where is waldo



Where is waldo



Where is waldo



Where is waldo

